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# A Method of Visualizing Mutual-Conductance Characteristics of Vacuum Tubes 

(Received April 20, 1951 )
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#### Abstract

How to visualize characteristics of mutual-conductance vs. grid-voltage of vacuum tubes on the fluoresent screen of a cathode-ray tube and the apparatus which are made under this conception are described.

\section*{I. Introduction}

Methods to know directly or indirectly the mutual-conductance of vacuum tube have been developed ${ }^{1)}$ and several instruments ${ }^{2)}$ which indicate simply by a meter have been accomplished during the past many years. Moreover, the ways to make characteristics of grid-voltage vs. plate-current or plate-current vs. plate-voltage visible are described by M. von Ardenne ${ }^{3)}$ and others. ${ }^{4}$ ) According to my method which will be explained later, characteristic curve of grid-voltage $e_{g}$ vs. mutualconductance $G_{m}$ can be traced on the fluoresent screen of a cathode-ray tube.

Plate-current is easy to change into potentials which are proportional to $i_{p}$ by putting a small resistance in the plate circuit. But as mutual-conductance is the ratio of plate-current to grid-voltage it has to be converted into a voltage which is proportional to the ratio. The apparatus made by means of this circuit can be used for testing of tubes in mass-production, the comparison of $G_{m}$ characteristics of two tubes and determination of the suitable working point of every tube in amplifier or in other miscellaneous circuit design. Moreover, it is very convenient to know $G_{m}$ in wide range, even when grid-voltage is positive.


## II. Action of Fundamental Circuit

The fundamental circuit of this instrument consists of the circuits which are: first, including tube to be tested, second, converting to voltage, third, amplifier and cathode-ray oscillograph as illustrated in Fig. 1. Notations are as follows:

[^0]
$V_{x}$ : Tube under test
$V_{1}, V_{2}$ : Amplifying tube having constant $G_{m}$ for varying input signal voltages $V_{3}, V_{4}$ : Amplifying tube which changes their internal resistance linearly with input signals
$V_{s}: \quad$ Constant-voltage glow-tube
$R: \quad$ A small constant load resistance in plate circuit of $V_{x}$
$G_{m}: \quad$ Mutual-conductance of $V_{x}$
$i_{p}$ : a. c. component of plate-current of $V_{x}$
$e_{g}: \quad$ Input a.c. grid-voltage of $V_{x}$
$e_{g 1}$ : Voltage which is proportional to $e_{g}$
$e_{g 2}$ : $\quad$ Out-put a.c. voltage which is developed across the load resistance $R$
A: Voltage amplification of $V_{1}$ and $V_{2}$
$E: \quad$ Constant d. c. potential between $V_{3}$ and $V_{4}$ which are connected in series
$r_{3}, r_{4}$ : Internal resistance of $V_{3}$ and $V_{4}$, respectively
$e: \quad$ Voltage appearing between plate and cathode of $V_{4}$
The tube $V_{x}$ which will act as an amplifying tube has the load resistance $R$. In this case, $R$ is a pure resistance and much smaller than other loads connected to the anode and also it must be small to avoide large d. c. voltage drop across the resistance. When a voltage $e_{g}$ applies to the control-grid of $V_{x}$ from the audio signal generator, over the resistance $R$ an output voltage $e_{g 2}$ appears. In general, $e_{g}$ is bigger than $e_{g 2}$ because of small $R$. Therefore the following equation will be derived.
\[

$$
\begin{align*}
e_{g 2} & =R i_{p}  \tag{1}\\
G_{m} & =\frac{\partial \mathrm{I}_{p}}{\partial E_{g}} E_{p}=\text { const. } \quad \because \frac{i_{p}}{e_{g}}=\frac{1}{R} \cdot \frac{e_{q 2}}{e_{q}}=\frac{1}{10 R} \cdot e_{q 2} \tag{2}
\end{align*}
$$
\]

where $R$ is constant.
$e_{g 2}$ is applied to the control-grid of $V_{1}$ by adjusting $R_{1}$ to be not over 1 volt. Also $e_{g}$ becomes $e_{g 1}$ passing through the transformer $T_{1}$ and their phase difference is just $180^{\circ}$. Then $e_{g_{1}}$ will be stepped down almost one tenth according to $R_{2}$ and will be applied to the grid of $V_{2} . V_{1}$ and $V_{2}$ are connected in push-pull. Since both $e_{g 1}$ and $e_{g 2}$ are in phase, output voltage across the transformer $T_{2}$ is proportional to the difference between $e_{g 1}$ and $e_{g 2}$.
$V_{1}$ and $V_{2}$ are pentodes having the same characteristics and by choosing the optimum grid-bias voltage, $G_{m}$ of both tubes may be made constant within about 2 volts for input grid voltages. Therefore output voitages in plate circuit of both tubes will be $A e_{g_{1}}$ and $A e_{g 2}$, according to the same amplification $A$, despite of small variation in grid inputs. Output voltage of $T_{2}$ will be $A\left(e_{y 1}-e_{f 2}\right) . V_{3}$ and $V_{4}$ are connected in series and are applied constant d.c. voltage $E$ between the plate of $V_{3}$ and cathode of $V_{4} . V_{3}$ and $V_{4}$ have identical characteristics, too. In this case pentode $V_{3}$ and $V_{4}$ are used as triode and are set with their grid-bias to the region where internal resistances are changing linearly with grid input voltages. To the control-grid of $V_{3}$ is applied the voltage which is proportional to $e_{g 2}$ but in opposite phase by $V_{3}$. To the $V_{4}$ the voltage which is proportional to $e_{g 1}-e_{g 2}$ is applied. Input voltages of both tubes are in phase. Internal resistance $\boldsymbol{r}_{3}, \boldsymbol{r}_{4}$, of $V_{3}, V_{4}$, respectively, are inversely proportional to their grid input voltages. Then,

$$
\begin{align*}
r_{3} & =K / e_{g 2}  \tag{3}\\
r_{4} & =K /\left(e_{g 1}-e_{g 2}\right) \tag{4}
\end{align*}
$$

where $K$ is the proportional constant of tubes.
The voltage $e$ between anode and cathode of $V_{4}$ is then given by the equation,

$$
\begin{equation*}
e=\frac{r_{4}}{r_{3}+r_{4}} \cdot E \tag{5}
\end{equation*}
$$

Substituting ( 3 ) and ( 4 ) into ( 5 ),

$$
\begin{equation*}
=\frac{\frac{K}{e_{g 1}-e_{y 2}}}{\frac{K}{e_{g 1}-e_{g 2}}+\frac{K}{e_{g 2}}} \cdot E=\frac{e_{q 2}}{e_{q 1}} \cdot E \tag{6}
\end{equation*}
$$

Comparing (2) with (6),

$$
\begin{equation*}
e \propto G_{m} \tag{7}
\end{equation*}
$$

Therefore $e$ is proportional to $G_{m}$ of $V_{v}$ by setting every circuit's element and tube constants to optimum corditions.

After amplifying, the voltage $e$ and $e_{g}$ are applied to vertical and horizontal axis of a cathode-ray tube, respectively. Then $G_{m}$ characteristics vs. grid-voltage is seen on the fluorescent screen of its tube.

## III. Practical Apparatus

The arrangement and connections of these circuits in practice are shown in Fig. 2.


Fig. 2.

An audio oscillator employed for a. c. source of $e_{y}$, can generate variable voltages from about 2 to more than 10 volts in good regulation and in pure sinusoidal wave forms, and its frequency can be changed $500 \mathrm{c} / \mathrm{s}$ to $5000 \mathrm{c} / \mathrm{s}$. Produced a. c. voltage may be always measured by a voltmeter. The next instrument including $V_{x}$ to be test has many sockets adapted for various types of tubes which we want to measure, like a tube checker. Moreover, two tubes of same kind; - one standard and the other to be tested - can be arranged on the board in order to compare their characteristics.

Output voltages of both tubes will be applied to the next circuit which is called " two phenomena switching circuit" to make it possible to see both curves simultaneously on the screen. Using the switching circuit, it is easy to choose tubes of the same characteristic as the standard tube from the coincidence of their curves. This may be used for mass-production at a factory. To determine the working point of tube, voltmeter and ammeter which indicate its plate-current, screen-voltage, plate-voltage and grid-bias voltage are placed in $V_{x}$ circuit.

The switching circuit ${ }^{5}$ consists of multivibrator and two amplifiers which are set almost at unity amplification. Its switching frequency is about $700 \mathrm{c} / \mathrm{s}$. So
(5) K. Izumikawa \& S. Oka; Cathode-ray Tubes and Oscillograph, Kyoritsusha, ( 1942 ).
it is better to choose second or higher harmonics of its frequency as input gridvoltage $e_{g}$ in order to stop drifting of the image of the screen.

The next is " converting circuit "'. This is the vitals in this method and is difficult to adjust all elements to their optimum conditions. Valve-voltmeter and cathode-ray oscillograph should be used for adjustment, that is to check potentials and wave forms in every point of the circuit to satisfy the conditions which have already been mentioned before. Unless $V_{1}, V_{2}, V_{3}$ and $V_{4}$ are operating at suitable point, various errors and distortions will arise.

To amplify $g_{g}$ and output voltage $e$ of the converting circuit, wide-band amplifiers are used. By changing the amplification the curve on the screen can illustrated smaller or larger optionally.

Amplified voltage $e_{g}$ and $e$ are applied to horizontal and vertical deflection plates of the cathode-ray tube, respectively. If there is some phase difference between both voltages, the curve appearing on the screen may display a loop similar to Lissajous figure. Though in the $V_{x}$ circuit there is a phase shifter, it can not make them coincide perfectly as a single curve.

To avoid the disagreement of the characteristic curve, " return diabling circuit " is employed. Negative rectangular pulse is applied between grid and cathode of the cathode-ray tube. Then it makes the returning curve disappear during the interval of $\frac{\pi}{2}$ and $\frac{3 \pi}{2}$ in input voltage $e_{g}$.

## IV. Results in Measurement

Several photos of $G_{m}$ characteristics which have been taken by this apparatus are shown in Fig. 3.


Fig. 3.
The photos were taken by this instrument, and vertical and horizontal axis are $\mathrm{G}_{m}$ and $\mathrm{e}_{g}$ respectively.


(d) 6K7, 6j7

Where ; $E_{p}=$ d. c. plate voltage, $E_{g}=$ grid-bias voltage,

Explanation of results are as follows:
Photo (a): $V_{x} ; 6 \mathrm{C} 6$ (No 1 ), $E_{p}=200$ volts, $E_{s ~}=100 \mathrm{v}$,

$$
E_{g}=-5 \mathrm{v}, \quad e_{g}=10 \mathrm{v}(\text { crest value }) .
$$

(b): $V_{x} ; 6 \mathrm{C} 6$ (No 1 ) \& ( No 2)

$$
\begin{aligned}
& E_{p}=285 \mathrm{v}, \quad E_{s g}=115 \mathrm{v}, \\
& E_{g}=-6 \mathrm{v} .
\end{aligned}
$$

Both have nearly the same characteristics.
(c): $V_{x} ; 6 \mathrm{C} 6$ ( No 1 ) \& ( No 3 ),

$$
\begin{aligned}
& E_{p}=275 \mathrm{v}, \quad E_{s g}=120 \mathrm{v} \\
& E_{g}=-6 \mathrm{v}
\end{aligned}
$$

No 3 tube was inferior to No 1 which was used as standard.
(d): $V_{x} ; 6 \mathrm{~K} 7 \& 6 \mathrm{~J} 7$,

$$
\begin{aligned}
& E_{p}=225 \mathrm{v}, \quad E_{s g}=80 \mathrm{v}, \\
& E_{g}=-4 \mathrm{v} .
\end{aligned}
$$

It is clearly to be seen in the picture 6K7's $G_{m}$ is bigger than that of 6 J 7 under the same conditions.

## V. About Errors

In this method an absolute value of $G_{m}$ will be hardly obtainable because of complicated adjustment. Even though all the adjusting elements of the whole circuits including vacuum tubes were set in optimum states, errors in the final
results would be less than $20 \%$ of the real values except the vicinity of the center in illustrated $G_{m}$ curve on the screen. If the exciting signal is made smaller, the resultant image may be nearer the real one.

Also $G_{m}$ of the same tubes have been measured by the well-known bridge circuit to compare with that taken by the risual method. $V_{1}, V_{2}, V_{3}$, and $V_{4}$ have been selected among a lot of tubes by using the bridge method.

Now, we must pay attention to the following to get more exact characteristics of $G_{m}$.

1) Characteries of $V_{1}, V_{2}$, and $V_{3}, V_{4}$ should be the same respectively and those tubes must be working under the same conditions. Concerning $V_{3}$ and $V_{4}$, input voltages are admitted under 3 volts. Especially care must be taken to select suitable grid-bias voltages for both cases.
2 ) Coupling transformer $T_{1}, T_{2}$, and $T_{3}$ must have high qualities - low resistance, low leakage inductance, low losses and higher satulation. This is in order to avoid amplitude and phase distortions while signals pass through the transformers.
3 ) Coupling condensers and dividing resistances may be selected with suitable values to avoid much phase difference.
2) $e_{g 1}$ must be bigger than $e_{g 2}$.

5 ) E should be kept always constant. Patteries as the d. c. source may be better, but rectified source using glow-tubes was sufficient to employ for this purpose.
Variation of the source voltage will cause drifting of the images.
6 ) Wave forms of input signals should be pure sinusoidal and after passing through $V_{x}, V_{1}, V_{2}, V_{3}$ and $V_{4}$ they should be as similar as possible. Amplitude of signal should not exceed over 10 volts (crest value). The smaller signals the more correct the curves will be.

## VI. Conclusion

This instrument will not be suitable for measurement of absolute mutual-conductance because of the reasons already mentioned above. Eut this is to be used for judgement of good or bad tubes and for determination of best operating point, morever it is very convenient to know the outline of tube characteristics in wider region extending over negative and positive grid-voltages. If the tube is inferior to the standard one, by changing grid-bias voltage or plate-voltage it can be used as a good one. Although the results are not very accurate, this can also be employed to know the dynamic characteristics of tubes by putting their load resistance instead of the smaller R.

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