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# Duration of Assets: <br> Examination of Directly Observed Discard Data in Japan 

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#### Abstract

Comprehensive investigation for discard and decay of assets has not been sufficiently implemented in Japan. As the first step for reframing measurement of capital stock in Japanese national accounts, we investigate discard patterns of asset, based on new micro data for directly observed discards (Survey of Actual Capital Stock and Discard of Private Enterprises: SASD), which is newly developed by ESRI (Economic and Social Research Institute, Cabinet Office) in 2003.

In this paper, we report the preliminary results of the Weibull family of distributions to approximate the discard patterns of 66 assets. The results indicate that almost half of assests has a progressively increasing hazard rate. For further investigations of discards, we provide some proposals to improve the design of questionnaire in the present SASD.


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## 1 Introduction

Japan's national accounts are moving toward a sweeping improvement of capital measurement, which may be one of the most problematic areas in the current accounts ${ }^{* 1}$. On reframing it, assumptions for duration of assets and decay of the surviving assets are the key factors to determine the accuracy of capital stock estimates. The objective of this paper is to examine actual survival distribution and asset service lives, based on the directly observed discard data that is newly implemented in 2003 by Economic and Social Research Institute (ESRI), the Cabinet Office (CAO), Japan.

In the National Wealth Survey (NWS), the Japanese government directly investigated detailed capital stocks owned by corporations, government, and households. The NWSs in 1955 and 1970 are the largestscale surveys for direct observation of capital stock (DOC). *2 The NWS is an unique method to directly attain actual gross capital stock and net capital stock in business account. However, at present, it may be difficult to finance an additional large-scale NWS. In addition, from the point of view of the theory of capital measurement, the net capital stock that can be observed in business accounts no longer provides appropriate measures for the wealth or productive capacity of capital stock, since it is based on tax-lives that can considerably differ from the actual service life of the asset. The significant role of the NWS may be the measurement of benchmark "gross" capital stocks that are surviving in the production process at the period of the investigation.
In order to measure gross capital stock without large-scale survey of DOC , we have to investigate

[^1]| Servey Year | Published Year | Organization | ref |
| :---: | :---: | :---: | :---: |
| 1905 | N.A. | Bank of Japan |  |
| 1910 | 1912 | Bank of Japan |  |
| 1913 | Oct. 1921 | Kokusuuin |  |
| 1917 | N.A. | Bank of Japan |  |
| 1919 | Oct. 1921 | Kokusuuin |  |
| 1924 | Feb. 1928 | Naikaku Tokeikyoku | estimates existent statistics |
| 1930 | Nov. 1933 | Naikaku Tokeikyoku | representative NWS before WWII |
| 1935 | Oct. 1948 | Naikaku Tokeikyoku | based on similar method of the 1930 survey |
| 1955 | Mar. 1958 | EPA | model for the NWS after WWII |
| 1960 | Dec. 1964 | EPA | survey at small scale |
| 1965 | Aug. 1967 | EPA | survey at small scale |
| 1970 | Feb. 1975 | EPA | survey at large scale |
| Source: Kokusu EPA $\rightarrow$ | conomic Plann $n \rightarrow$ Naikaku conomic and S | g Agency (1976). keikyoku $\rightarrow$ Statisti ial Research Institur | Bureau, MIC (present). Cabinet Office (present). |

duration of assets. One approach to recognize the durability is a sample survey for actual discards of assets in business account. In Japan, ESRI implemented the Survey of Actual Capital Stock and Discard of Private Enterprises (SASD) in 2003, as the first trial towards the revision of capital stock. In this paper, we report the results of our examination using this sample survey. In addition, for the future investigations of discards, we provide some proposals to improve the design of questionnaire in the present SASD.

Another approach to recognize discard patterns is the use of registration data for some particular assets (e.g. motor vehicles), which are obligated to be registered to government for its usage. It can provide complete dataset to describe the number of surviving assets used by companies or households. In this paper, we also report the estimates based on the registration data for motor vehicles to compare with our results based on the SASD.

In section 2, we start to clarify the terminologies used in this paper. The methodology to approximate discard patterns is briefly introduced in section 3. In this paper, the Weibull distribution with two parameters is assumed. We introducenewly implemented data for directly observed discard and examined its properties in section 4. Our preliminary results based on SASD for 66 assets and registration data for motor vehicles are reported in section 5 . Section 6 concludes briefly, with the proposals for improving the directly observed discard survey for further research.

## 2 Terminology

### 2.1 Capital Stock: Gross, Productive, and Net

The terminologies to represent capital stock and discard/decay may still confuse readers. In this section, we begin with the clarification of the terminologies used in this paper.

Traditionally, two distinctive concepts for capital stock, gross capital stock and net capital stock, were used. The distinction of the two concepts is based on depreciation. Gross capital stock is defined before the deduction of depreciation, and net capital stock is reduced by the depreciation. As the traditional gross concept still remains in the Japanese statistics of capital stock for production analysis, gross capital stock may have been sometimes thought suitable to measure the productive capacity of capital. However, the traditional system of gross and net capital stock is incapable of portraying the two different aspects of capital, except under unrealistic assumptions. This was finally abandoned by BEA in 1997 (see Fraumeni, 1997; Katz and Herman, 1997; and BEA, 2003), a quarter century after the controversy between JorgensonGriliches (1972) and Denison, as Jorgenson (1989) had clearly pointed this out.

The intensive works of Dale W. Jorgenson, Robert E. Hall, Zvi Griliches, Charles R. Hulten, Walter E. Diewert, Jack E. Triplett, and many other researchers and statisticians, have developed the theory for measurement of capital and accumulated the empirical results. The theory of capital measurement clarifies
the distinction of these two aspects of capital, based on the concepts of age-efficiency profile (AEP) and age-price profile (APP). We use three distinctive stock concepts in this paper: gross, productive, and net capital stocks. ${ }^{* 3}$

### 2.2 Aging of Assets: Discard and Decay

There may be a consensus about the use of "retirement" or "discard," which are used synonymously. Here, we describe the distinction between discard and decay, to clarify the objective of this paper in our reframing measurement of capital stock.

In the OECD manual on measuring capital, Blades (2001) uses "retirement" and "discard" interchangeably to mean the removal of an asset from the capital stock, with the asset being exported, sold for scrap, dismantled, pulled down, or simply abandoned. Also, retirements and discards are distinguished from "disposals" which include sales of assets as second-hand goods for continued use in production."4
Jack E. Triplett (1997) also gives the definition. He defines the term "deterioration" to represent the relative efficiency in the age-efficiency profile (AEP). Deterioration arises from two sources: "retirement" and "decay," which is defined by the loss of efficiency of a surviving asset. Retirement designates assets withdrawn from service. Also, he uses "discards" or "scrapping" synonymously.
In the framework for measuring productive capital stock, the key idea is the AEP. Based on the comprehensive empirical studies of Hulten and Wykoff (1981a, 1981b, 1981c), the geometric distribution as the AEP or APP is approximately accepted for many assets in the U.S. Also, Nomura (2004, ch-2) estimates

[^2]depreciation rates based on the Box-Cox transformed APP, using data in the second-hand market for motor vehicles, and the AEP using data in the rental markets for housing in Japan. The geometric approach is accepted as an approximation for these assets. In the Hulten-Wykoff methodology, the AEP represents a combined profile of discard and decay or the distribution of deterioration by Triplett's terminology.

Our measurement on duration of assets have two meanings in this context. Firstly, if the geometric approach can adequately approximate the AEP, the investigation only for the discards may have less meaning. However, it may be usually difficult to investigate the AEP for many kinds of assets, due to the lack of adequate market data for aged assets. In fact, there is sometimes no actual market for aged assets. Second, some assumption for discards is required to estimate the AEP using market price data for aged assets, since the observed data at the market is censored because of the lack of the data for the assets that already retired at the period of the investigation. In the comprehensive studies of Hulten and Wykoff, they assume the Winfrey distributions to adjust the censored samples.

## 3 Methodology

### 3.1 Distribution for Discard Pattern

Discard patterns of assets are frequently approximated by some probability distribution function, due to the difficulties of directly observed data to attain actual gross capital stock. ${ }^{* 5}$ This section briefly depicts particular functions used to approximate discard pattern and outlines the Weibull family of distributions that is mainly assumed in this paper.

Blades (2001) discusses four types of distribution - simultaneous exit (SE), linear (LR), delayed-linear (DL), and bell-shaped (BS). As the BS-type functions, logistic, Winfrey, hyperbolic, Weibull, log-normal, and so forth are widely used. In Japan, at the Gross Capital Stock of Private Enterprises (GCSPE) that describes gross capital stock by industry, ESRI assume the SE, in which all assets will be simultaneously retired when the age of asset reaches the end of its service life.* However, the SE is widely recognized that it may be the most inappropriate retirement pattern. Blades (2001) indicates that the SE and LR are clearly unrealistic and that the DL and BL gives more realistic model. ${ }^{*}$

[^3]At the second meeting of Canberra Group on Capital Stock Statistics in September 1998, Meinen, Verbiest, and Wolf (1998) reports their examination on the alternative estimates of gross capital stock assuming the SE, DL, hyperbolic, logistic, and Weibull distributions, compared with actual measurement of capital stock in the Netherlands. They conclude the estimates assumed the SE does not reproduce the older vintage classes sufficiently enough and that the DL or the BS-type survival functions with a longer tail perform better.

### 3.2 Weibull Distribution

To approximate discard patterns, we assume the Weibull family of distributions. The probability density (mortality) function $f(\tau)$, cumulative distribution function $F(\tau)$, and survival function $S(\tau)$ of the Weibull distribution are:

$$
\begin{align*}
& f(\tau)=\alpha \lambda^{-\alpha} \tau^{\alpha-1} e^{-\left(\frac{1}{\lambda}\right)^{\alpha}}  \tag{1}\\
& F(\tau)=\int_{0}^{\tau} f(t) d t=1-e^{-\left(\frac{2}{\lambda}\right)^{\alpha}},  \tag{2}\\
& S(\tau)=1-F(\tau)=e^{-\left(\frac{2}{\lambda}\right)^{\alpha}} \tag{3}
\end{align*}
$$

where $\tau$ is the continuous age and $\lambda$ and $\alpha$ are known as the scale and shape parameters $(\lambda>0$ and $\alpha>0) .{ }^{* 8}$ The Weibull distribution is more flexible than the exponential distribution, since it is the exponential distribution of the power transformed age: $\tau^{\alpha}$. In the special case of $\alpha=1$, the Weibull distribution is identical with the exponential distribution, which has the constant rate of retirement. Figure 1 displays $f(\tau)$ and $S(\tau)$ for the cases of $\alpha=0.5,1,2,3$, under $\lambda=10$.

The $k$-th moment $m_{k}$ of the Weibull probability density function $f(\tau)$ is given as:

$$
\begin{equation*}
m_{k}=\lambda^{k} \Gamma\left(1+k \alpha^{-1}\right) \tag{4}
\end{equation*}
$$

where $\Gamma()$ is the gamma function, which is defined as $\Gamma(x)=\int_{0}^{\infty} e^{\mu} \mu^{x-1} d \mu$. The 1st moment gives the

[^4]

Fig. 1 The Weibull Density and Survival Functions
average service life $T$ :

$$
\begin{equation*}
\bar{T}=m_{1}=\lambda \Gamma\left(1+\alpha^{-1}\right) . \tag{5}
\end{equation*}
$$

For the case of $\alpha=1$ or $\alpha=\infty$, average service life $\bar{T}$ is identical with the scale parameter $\lambda$ since $\Gamma(2)=\Gamma(1)=1$. For the cases of $\alpha=1 / 2,1 / 3,1 / 4$, average service life $T$ is $2 \lambda, 6 \lambda, 24 \lambda$, respectively, using the property of the gamma function: $\Gamma(x+1)=x \Gamma(x)$. Roughly, $f(\tau)$ is positively skewed (left-skewed) for $\alpha<2.6$, approximately symmetric for $2.6<\alpha<3.7$, and negatively skewed (right-skewed) for $3.7<\alpha .{ }^{\circ} 9$ As retirement patterns of assets, the shape parameter $\alpha$ may be mostly between 1 and 3 , so that the

[^5] of the mean, median, and mode of the Weibull density function. The $y$-axis scale times $\lambda$ represents each value.

average service lives are a little bit small value of the scale parameter $\lambda$, since $\Gamma\left(1+\alpha^{-1}\right)$ has its minimum value 0.8856 for $\alpha=2.16$ and $0.8856 \lambda \leq T \leq \lambda$ for $1 \leq \alpha \leq \infty$.

Also, the standard deviation of asset service life: $\sigma_{T}$ is given:

$$
\begin{equation*}
\sigma_{T}=\left(m_{2}-m_{1}^{2}\right)^{1 / 2}=\lambda\left(\Gamma\left(1+2 \alpha^{-1}\right)-\Gamma\left(1+\alpha^{-1}\right)^{2}\right)^{1 / 2} \tag{6}
\end{equation*}
$$

For the case of $\alpha=1, \sigma_{T}$ is also $\lambda . \sigma_{T}=\infty$ as $\alpha \rightarrow 0$, and $\sigma_{T}=0$ as $\alpha \rightarrow \infty$.
The Weibull hazard function $h(\tau)$, and cumulative hazard function $H(\tau)$ are:

$$
\begin{align*}
& h(\tau)=\frac{f(\tau)}{S(\tau)}=\alpha \tau^{-1}\left(\frac{\tau}{\lambda}\right)^{\alpha}  \tag{7}\\
& H(\tau)=\int_{0}^{\tau} h(t) d t=-\ln (S(\tau))=\left(\frac{\tau}{\lambda}\right)^{\alpha} \tag{8}
\end{align*}
$$

For the case of $\alpha=1$, the hazard rates $h(\tau)$ are constant as $\lambda^{-1} \cdot{ }^{10}$ As $\tau$ increases, the hazard rate decreases for $\alpha<1$ and increases for $\alpha>1$. Figure 2 displays $h(\tau)$ and $H(\tau)$ for the cases of $\alpha=0.5,1,2,3$, under $\lambda=10$. In the case of $\alpha=2$, the hazard rate in Figure 2(a) increases linearly.

Taking logarithm of the Weibull cumulative hazard function in the equation (8), it can be written as a linear equation:

$$
\begin{equation*}
\ln H(\tau)=\beta+\alpha \ln \tau \tag{9}
\end{equation*}
$$

where $\beta=-\alpha \ln \lambda$. This log-linear relationship of the cumulative hazard and age makes the estimation model easy to handle.

## 4 Data and Actual Duration

### 4.1 SASD

The data used in this paper is the Survey of Actual Capital Stock and Discard of Private Enterprises (SASD), which is newly developed by ESRI, CAO. As the first step to sweepingly revise the capital measurement in the Japanese national accounts, ESRI implemented the SASD in 2003. This investigates the actual capital stock and discard for the 2002 fiscal year. This survey (hereafter 2002-SASD) provides primary
*10 A precise definition of the hazard function in terms of probabilities is

$$
h(\tau) \equiv \lim _{h \rightarrow 0} \frac{P(\tau \leq T<\tau+h \mid T \geq \tau)}{h}
$$

By this definition, the hazard function is also called as the conditional failure density function. To obtain the cumulative hazard function in the equation (8), the hazard function can be rewritten as

$$
h(\tau)=\frac{\lim _{h \rightarrow 0}(P(\tau \leq T<\tau+h) / h)}{P(T \geq \tau)}=\frac{\left.\lim _{h \rightarrow 0}(F(\tau+h)-F(\tau)) / h\right)}{1-F(\tau)}=\frac{f(\tau)}{S(\tau)}=\frac{-S^{\prime}(\tau)}{S(\tau)}=-\frac{d \ln (S(\tau))}{d \tau}
$$



Fig. 2 The Weibull Hazard and Cummulative Hazard Functions
results as the first trial to investigate duration of assets. Hence, it is one of our objectives for this paper to locate the problems within the 2002-SASD, in order to improve the design of questionnaire for the future investigations. In this section, we introduce the outline of the 2002-SASD and its properties.
The objective of the 2002-SASD is to directly observe the capital stock and discards of private enterprises. The target population is the private enterprises with over thirty million yen of the (financial) capital stock at their business accounts. The number of samples in the 2002-SASD is 5,880 companies (the sampling rate is 4.3 percent), by random sampling method from the stratified populations by five capital groups $\times$ twenty-nine industries. The number of effective responses is 2,903 (the response rate is 49.4 percent).
The 2002-SASD consists of two kinds of investigations. The first is the survey of capital stock, investment, depreciation, purchases of second-hand assets, and discards by five capital groups and by eight asset groups of the private enterprises, which are classified to twenty-nine industries. ${ }^{41}$ The first investigation is similar to the Financial Statements Statistics of Corporations (FSSC), produced by Policy Research Institute, Ministry of Finance (MOF), although the 2002-SASD has much smaller samples than the FSSC. ${ }^{* 12}$

[^6]The second investigation of the 2002-SASD provides more detailed data for discards of assets owned by private enterprises. Here, assets are classified into eight asset groups. In each asset group, the three major assets retired in the 2002 fiscal year are investigated, with the periods of the purchase and the retirement, and the asset value at the period of the purchases. It makes possible to figure out the completed duration data of assets. Moreover, the assets sold as second-hand goods for continued use in production are identified in the 2002-SASD to define relevant service lives of assets. ${ }^{* 13}$

On the other hand, to describe appropriate discard patters, the retired assets that were origianlly purchased as second-hand goods should be excluded, since the mixture lets the average service lives be biased downwardly. However, in the 2002-SASD, there is no questionnaire if the retired asset was new or second-hand at the period of the purchase, as long as company does not report an additional information at the questionnaire. This point has to be revised at the future investigation.

The kinds of assets to be reported are not designated in particular at the questionnaire of the 2002SASD. Therefore, company could choose arbitrarily three assets from the wide range of the assets within each asset group. Although this open questionnaire makes it possible to collect data for a number of assets, the non-specification of asset also makes it difficult to control the differences in quality of the asset samples, even if they might be considered as a class of asset. In fact, it is sometimes difficult to let asset samples correspond to a class of asset if the reported names are not clear. In addition, sampling bias in the 2002-SASD should be considered. We depicted it in section 4.3, after describing the actual age-survival distributions from this data.

### 4.2 Actual Age-Survival Distribution

Based on the directly observed discard data in the second investigation of the 2002-SASD, we estimate the actual age-survival distribution in three ways (the last one is defined in equation (20) in section 4.4, later). Let $\tau$ and $v$ are column vectors denote the duration period and the value at the period of the purchase, respectively. Here, the duration period is defined only for the retired asset, excluding the assets sold as second-hand goods. $\tau_{i}$ and $v_{i}$ are the components for asset samples $i$ that belong to a given class of asset. The original data of $v_{i}$ in business account is evaluated by the historical price at the period of the purchase. Here, we reevaluate $v_{i}$ by the constant prices using the price index in each asset. ${ }^{-14}$

[^7]The first actual survival distribution is simply approximated as:

$$
\begin{equation*}
S_{0}(\tau) \approx \frac{\mathbf{j}^{\prime} \mathbf{i}}{\mathbf{i}^{\prime} \mathbf{i}}=\mathbf{j}^{\prime} \mathbf{w}_{0}, \tag{10}
\end{equation*}
$$

where $i$ stands for the column vector consisting of $1 s$, so that $i^{\prime} i$ is the number of samples $N$. Hence, $w_{0}$ is the column vector consisting of the same simple weights $1 / N$. The components $j_{i}(\tau)$ in the column vector j are defined as:

$$
j_{i}(\tau)= \begin{cases}1 & \text { if } \tau_{i} \geq \tau  \tag{11}\\ 0 & \text { otherwise }\end{cases}
$$

Therefore, the number of assets survived at age $\tau$ is $j^{\prime} i . S_{0}(\tau)$ is defined as the actual survival distribution used the simple weights for each sample, regardless of the differences in the values $v_{i}$. Here, the average service life is defined as

$$
\begin{equation*}
T_{0}=\tau^{\prime} \mathbf{w}_{0} . \tag{12}
\end{equation*}
$$

The second actual survival distribution $S_{v}(\tau)$ is approximated as

$$
\begin{equation*}
S_{v}(\tau) \approx \mathbf{j}^{\prime} \mathbf{w}_{v} \tag{13}
\end{equation*}
$$

where $w_{v}$ represents the weights for sample $i$, formed by the column vector consisting of $w_{i}(\tau)$, as

$$
\begin{equation*}
\mathbf{w}_{v}=\frac{\mathbf{v}}{\mathbf{i}^{\prime} \mathbf{v}} \tag{14}
\end{equation*}
$$

The real value weights $\mathbf{w}_{v}$ are expected to adjust the differences in the quality among samples $i$. In the questionnaire of the 2002-SASD, companies may sometimes report the total value of the retired assets, although it is expected that the assets were purchased and retired at the same periods. However, there is no questionnaire to report the number of assets in the 2002-SASD. The differences in the numbers among $i$ may be somewhat adjusted by the use of weights $w_{v}$. The average service life in the second definition is

$$
\begin{equation*}
T_{v}=\tau^{\prime} w_{v} . \tag{15}
\end{equation*}
$$

The two actual survival distribution $S_{0}(\tau)$ and $S_{v}(\tau)$ provide the different pictures for an asset. Figure 3 displays $S_{0}(\tau)$ and $S_{v}(\tau)$ for the case of personal computers (PC) with the sample size $N=224$. In $S_{0}(\tau)$, the samples are well apportioned. On the other hand, some samples have large impacts around 4 ages in $S_{v}(\tau)$. In the case of PC, this may be due to the large number of assets reported in a single questionnaire. Although $S_{0}(\tau)$ looks more appropriate as the PC's survival distribution, the average service life $\bar{T}_{0}$ is 7.2 years, which is 80 percent higher than the PC's tax-life of 4 years. This seems too high. On the other hand, $T_{v}$ is 5.4 years, reflected the large-number of samples around 4 ages. It may be more adequate.

Bank of Japan, for each asset. The CGPI was named as Wholesale Price Index (WPI) before it has been greatly revised in 2000.


Fig. 3 Actual Survival Distribution: Personal Computers: $S_{0}(\tau)$ and $S_{v}(\tau)$

Figure 4 displays the actual survival distributions for office buildings, where $N=261 . S_{0}(\tau)$ seems linearly distributed in Figure 4(a). However, in Figure 4(b), some samples with 31 ages have significant impacts on the shape of $S_{v}(\tau)$. In this case, it may be due to the large-scale office buildings. The average service lives $T_{0}$ and $T_{v}$ are 15.4 and 22.2 years, respectively. Contrary to the case of $\mathrm{PC}, \bar{T}_{0}$ for office buildings may be too small.


Fig. 4 Actual Survival Distribution: Office Buildings: $S_{0}(\tau)$ and $S_{v}(\tau)$

For measuring gross capital stock, $S_{v}(\tau)$ may be preferred. If a number of assets retired at the same period, they should be counted separately. In addition, if a large-scale asset tends to provide a longer service life because of the superior durability, the difference of the scale should be considered in estimating
the average service life. Or, if it is possible to measure investment by the structure and scale of an asset, the survival distribution should be distinguished based on its classification.

### 4.3 Sampling Bias in SASD

Next, we examine the samples in the SASD. Let $I_{t}$ denote the quantity of investment of a single asset at the period $t$. Figure 5 represents two samples invested at the periods $t_{1}$ and $t_{2}$ and these discard patterns that are assumed to follow the identical probability density function (pdf) $f(\tau)$, regardless of the difference in their vintages. At the period of the survey $t\left(t \geq t_{1}, t_{2}\right), f\left(t-t_{1}\right) I_{t_{1}}$ and $f\left(t-t_{2}\right) I_{t_{2}}$ are retired for sample-1 and sample-2, respectively. By the single-period survey like the SASD, the discard data sets $f\left(t-t_{i}\right) I_{t_{i}}$ of the assets with different vintages $t_{i}$ can be observed.


Fig. 5 Discard Data Collected at the Single-Period Survey

We define the "pseudo" pdf $f_{t}^{\prime \prime}(\tau)$ based on the collected discard data at the period of $t$ as:

$$
\begin{equation*}
f_{t}^{*}\left(\tau_{i}\right)=f\left(t-t_{i}\right) I_{t_{i}}=f\left(\tau_{i}\right) I_{t-\tau_{i}} . \tag{16}
\end{equation*}
$$

If $I_{t-\tau_{i}}$ is constant over vintages $t_{i}$ (or ages $\tau$ ) as shown in Figure 5, the pseudo pdf $f_{t}^{\prime}(\tau)$ is proportional to the "true" pdf $f(\tau)$. If not, the pseudo $f_{t}^{\prime \prime}(\tau)$ may be biased.

Figure 6 gives another picture of sampling in the SASD. The collectable samples in the 2002-SASD are the assets retired from April 2002 to March 2003. In this period of the investigation, the duration data (1) and (2) can be collected, but data (3) is not collected. ${ }^{* 15}$ The curves (a)-(e) in Figure 6 represent past investment

[^8]patterns $I_{t_{i}}$ at the periods $t_{i}(\leq t)$. In the case of (a), quantity of investment is constant, regardless of the difference in its vintage $t_{i}$. Thus the true pdf $f(\tau)$ can be estimated without biases, based on the pseudo pdf $f_{t}^{*}(\tau)$ in the equation (16).

In the case of (b), investment has a boom in the recent period. In the survey period $t$, the data with shorter service lives may be collected more. As the results, the average service life based on the collected samples may be underestimated. Even in this case, if the true service life of the asset is enough long not to operate the observable sample like data-(3), the bias may be negligible. In the case of (c), the data which has the linearly upward trend of investment results the downward biases in estimate for average service life. Especially, in the case of (d), the sample for a new product may be censored. Contrastively, if the actual investment has a downward trend like (e), the estimated average service life may be biased upwardly. "16


Fig. 6 Samples in the 2002-SASD and Investment Patterns

The method to eliminate this sample bias is to construct longitudinal data from the period of acquisition of an individual asset $t_{i}$ to the period to be retired $t$. Companies originally have complete individual records in all assets they own. If we make use of these complete data sets, the biases except the case of

[^9](d) can be diminished. Another complete data can be provided by registration data. Some particular assets like motor vehicles are regulated to be registered. The use of the registration data makes us to describe a complete discard pattern, if we could approximately neglect the difference in qualities of the asset samples. Section 5.2 provides our preliminary results based on the complete registration data for motor vehicles, to compare our results based on the 2002-SASD.

Another solution is to make a pooling data over periods. Multi-period surveys may make it possible to identify the effects of age $\left(\tau_{i}\right)$ and vintage $\left(t_{i}\right)$ separately, to appropriately estimate the true pdf. Or, using the samples investigated in different periods, we could define the integrated pseudo pdf, which is simply summed up among samples in different periods $t$, as

$$
\begin{equation*}
f_{\Sigma t}^{*}\left(\tau_{i}\right)=\sum_{t} f\left(\tau_{i}\right) I_{t-\tau_{i}}=f\left(\tau_{i}\right) \sum_{t} I_{t-\tau_{i}}=f\left(\tau_{i}\right) \Phi_{\tau_{i}} \tag{17}
\end{equation*}
$$

It can eliminate the bias to estimate the true $f(\tau)$ as $t \rightarrow \infty$, thanks to

$$
\begin{equation*}
\lim _{t \rightarrow \infty} \frac{\Phi_{\tau_{i}}}{\Phi_{\tau_{i}+\Delta}}=\frac{\Phi_{\tau_{i}}}{I_{t-\left(\tau_{i}+\Delta\right)}+\Phi_{\tau_{i}}}=\frac{1}{I_{t-\left(\tau_{i}+\Delta\right)} / \Phi_{\tau_{i}}+1}=1 \tag{18}
\end{equation*}
$$

As the samples in different periods are pooled, $\Phi_{\tau_{i}}$ can be treated as approximately constant and the biases may be reduced even in the case of non-stationary investment, under the assumption that the true pdf is unchanged over periods.

### 4.4 Adjustment to the Data from Single-Period Survey

Although multi-period survey is required to eliminate the biases, we examine a tentative adjustment to the single-period data in the 2002-SASD. We define the weights $\hat{\boldsymbol{w}}_{v}$, which consists of $\hat{w}_{i}(\tau)$, as

$$
\begin{equation*}
\hat{w}_{v}=\frac{\mathbf{v}\langle\mathbf{a}\rangle}{\mathbf{a}^{\prime} \mathbf{v}} \tag{19}
\end{equation*}
$$

where $\mathbf{a}$ is the column vector consisting of the adjustment coefficients $a_{i}$ and $<\cdot>$ is used to denote a diagonal matrix. As the adjustment coefficients $a_{i}$, we use the inverse of the quantity index of investment with the different vintages $\left(t_{i}\right)$, to reduce the bias in the equation (16).
The adjusted actual age-survival distribution and average service life are :

$$
\begin{align*}
& S_{\bar{v}}(\tau) \approx \mathrm{j}^{\prime} \hat{\boldsymbol{w}}_{v}  \tag{20}\\
& \mathrm{~T}_{\bar{v}}=\tau^{\prime} \hat{\boldsymbol{W}}_{v} . \tag{21}
\end{align*}
$$

In the case of PC, we define $a_{i}$, approximately using the actual private investment of computers and peripherals at the constant price estimated in Nomura (2004). Figure 7 reports the quantity index of investment $1 / a_{i}$ and the adjusted actual survival distribution $S_{v}(\tau)$ (the smaller dots represent $S_{v}(\tau)$ in

Figure 3(b)). An upward trend in the PC's actual investment is substantial as shown in Figure 7(a). By the adjustment, the weight of the data with a shorter service life is reduced and one with a longer service life is emphasized. Thus, the adjusted distribution of the PC is more durable than $S_{v}(\tau)$. The adjusted measure of the asset service life $T_{\hat{0}}$ is 6.2 years, which is between 7.2 (for $S_{0}(\tau)$ in Figure 3(a)) and 5.4 years (for $S_{v}(\tau)$ in Figure 3(b)). ${ }^{17}$


Fig. 7 Adjusted Actual Survival Distribution: Personal Computers: $S_{\widehat{D}}(\tau)$

Figure 8(a) represents the adjusted actual survival distribution of the office buildings (the smaller dots display $S_{v}(\tau)$ in Figure 4(b)), based on the similar adjustment procedure. ${ }^{18}$ The investment of the office buildings has a boom in the late 1980s, when the Japan was in the bubble economy. After this adjustment of the samples, the asset service life is 23.0 years, which is higher than 15.4 (for $S_{0}(\tau)$ in Figure 4(a)) and 22.2 years (for $S_{0}(\tau)$ in Figure 4(b)).

### 4.5 Actual Average Service Lives

Next, we estimate the asset service lives for all assets, in the three definitions: $\bar{T}_{0}, \tilde{T}_{v}$, and $T_{\vec{v}}$. Based on the 2002-SASD, we set 66 assets: 6-14.metal products, 15-33.general machinery, 34-47.electric machinery, 48-52.transportation equipment, $53-57$.precision machinery, $60-66$.buildings and construction. Table 2 reports the estimated results.

[^10]

Fig. 8 Adjusted Actual Survival Distribution: Office Buildings: $S_{\tilde{v}}(\tau)$

In general machinery, the assets that have shorter service lives are 31.copy machines ( $\bar{T}_{0}=7.9$ ), 22.semiconductor making equipment (9.2). In electric machinery, 38.personal computers (7.2), 39.mainframes and servers (7.4), 40.wired communication equipment (9.2), and 41.wireless communication equipment (9.8) have shorter lives. ${ }^{* 19}$ It may be reasonable that the IT-related assets have shouter service lives, reflecting the rapid technological progress.
The large differences between $T_{0}$ and $T_{v}$ are observed in buildings and construction and some of general machinery. That may imply that large-scale assets have a longer service life, reflecting the difference in the quality. Table 2 also represents some descriptive statistics for the service lives: median, minimum, maximum, and standard deviation. The minimum service lives for many assets are less than a few years. Even in buildings and construction, we could find a number of temporary buildings to be used for construction or display, although they are the small-scale assets. It may be important to consider the difference in the scales among samples.

## 5 Measurement

### 5.1 Results on the 2002-SASD

Based on the actual survival distributions defined as $S_{0}(\tau), S_{v}(\tau)$, and $S_{\bar{v}}(\tau)$ in section 4, we estimate the parameters of the Weibull distribution. Equation (9) gives the estimation model of the $\log$-linear relationship between the age and the cumulative hazard. Figures 11-16 show the actual age-survival

[^11]distribution $S_{0}(\tau)$ and the approximation by the Weibull distribution in each asset. Undoubtedly, the simultaneous exit can not any proper approximation for all assets. Tables 3, 5, 7 report the estimated parameters, based on $S_{0}(\tau)\left(\right.$ Case-1), $S_{v}(\tau)$ (Case- 2 ), and $S_{v}(\tau)$ (Case-3), respectively. Also, Tables 4, 6, and 8 represent age-survival profile of assets defined by the estimated Weibull distribution in each case.


Fig. 9 Distributions of Estimated Parameters: $\alpha$ and $\lambda$

Comparison of the parameters estimated in each case is reported in Figures 9 and 10. In Case-1, $\lambda$ is between 10 and 20 in many assets. As we described the properties of scale parameter $\lambda$ in section 3.2, average service life $\bar{T}$ is a little bit smaller than $\lambda$, where $T=\lambda \Gamma\left(1+\alpha^{-1}\right)$. If the difference in the scales (and probably the number of assets) is considered, $\lambda$ or $\bar{T}$ distributes in more wide range as represented in the comparison between Figure 9 (a) and 9 (b), emphasizing the large-scale assets with a longer service life. After the adjustment of the bias in the 2002-SASD, $T$ tends to be slightly longer in Case-3, as shown in Figure 10(d).
Although $\alpha$ is between 1.0 to 2.5 in many assets in Case-1, it varies widely in Case-2 and Case-3. $\alpha$ is a parameter to determine the hazard rates of assets, as represented in Figure 2(a). In the estimated results in the Netherlands (Meinen, Verbiest, and Wolf, 1998), the hazard rates in many assets tend to be regressively increasing ( $1<\alpha<2$ ), except in computers. Computers have a progressively increasing hazard rate ( $\alpha>2$ ). In our results of Case-3, almost half of assets has a progressively increasing hazard rate. This may give properties on discard patterns in Japan, in comparison with the Netherlands.

### 5.2 Alternative Estimate: Registration Data

At the ESRI's National Wealth Division and Keio Economic Observatory (KEO), we are preparing the use of registration data for particular assets to recognize more adequate discard patterns in Japan. To


Fig. 10 Comparison of Estimated Parameters: $\alpha$ and $T$
compare the estimated results from different data sources, we introduce our preliminary results based on the Japan's registration data for passenger cars and trucks at the end of March 2004. ${ }^{20}$ There are two outstanding properties in the use of registration data. Firstly, all data for the motor vehicles which have a car license in Japan are collected. The number of possessed vehicles in March 2004 is 42,624,206 for passenger cars (excluding light vehicles) and $7,276,081$ for trucks. Second, it can provide complete

[^12]longitudinal data of duration, so that we could describe the actual picture of age-survival distribution.
Table 1 compares the estimated Weibull parameters ( $\alpha$ and $\lambda$ ) and average service lives ( $T$ ) based on the 2002-SASD and 2004-registration data. In the estimates using registration data, the hazard rates in passenger cars and trucks are progressively increasing ( $\alpha>2$ ). Also, the estimates of $T$ are very similar to our estimates in the 2002-SASD. Although the registration data includes vehicles owned by households and does not reflect the difference in the qualities of vehicles, our estimates in the 2002-SASD seems appropriate.

Table. 1 Comparison of Parameters in Motor Vehicles: 2002-SASD and 2004-Registration Data

|  | Passenger Cars |  |  | Trucks |  |  |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: |
|  | $\alpha$ | $\lambda$ | $T$ | $\alpha$ | $\lambda$ | $T$ |
| Registration Data | 2.16 | 12.3 | 10.9 | 2.12 | 12.6 | 11.2 |
| 2002-SASD |  |  |  |  |  |  |
| Case-1 | 2.17 | 9.6 | 8.5 | 2.02 | 14.6 | 13.0 |
| Case-2 | 2.32 | 10.0 | 8.8 | 2.40 | 12.2 | 10.8 |
| Case-3 | 2.32 | 11.5 | 10.2 | 2.20 | 12.4 | 11.0 |

## 6 Concluding Remarks

As the first step for reframing measurement of capital in Japanese national accounts, we investigated the discard patterns by asset in this paper, based on the newly developed data for directly observed discards by ESRI: 2002-SASD. To improve our estimates and remove sample bias in the single-period survey, further continuous investigations on discards are required. Although we investigated the age-survival distributions in 66 assets, the difference in economic activities was not treated in this paper, due to the constraint of the sample size in each industry. However, we could find the average service life of PC may be somewhat longer in manufacturing sector than service sector.
For further investigation, the design of questionnaire in the 2002-SASD should be reconsidered: (1) It should be identified if the retired asset was originally new or second-hand at the period of the purchase. Without this identification, the asset service life may be biased downwardly; (2) The value of sold asset should be investigated based on the price at the period to be sold. It may make possible to produce estimates of age-price profile of the asset. (3) If company reports the aggregated value of retired asset, the number of asset should be investigated; (4) For some assets that considerably differ its qualities, e.g. buildings and construction, the questionnaire to recognize its characteristics is required, if it is possible; and (5) Investigation for intangible assets should be added.

In addition to the estimation based on the SASD, we plan to examine the different data sources. As we briefly report preliminary results for the passenger cars and trucks in this paper, the use of registration data may be preferable. By the use of the registration data, we may investigate the shift of age-survival distribution over periods.

Table. 2 Average Service Lives and Other Descriptive Statistics

|  |  | To | To | $\bar{T}_{\overline{0}}$ | smpl | median | min | max | stdev |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Woods Products | 7.2 | 8.0 | 8.0 | 13 | 6.1 | 3.4 | 18.3 | 3.8 |
| 2 | Furniture | 10.4 | 9.7 | 10.1 | 309 | 9.3 | 0.1 | 32.8 | 6.8 |
| 3 | Steel Pipes and Tubes | 17.3 | 17.2 | 17.5 | 47 | 15.8 | 2.3 | 41.3 | 10.6 |
| 4 | Electric Wires and Cables | 9.9 | 11.2 | 11.2 | 43 | 7.7 | 1.3 | 42.6 | 8.0 |
| 5 | Optical Fiber Cable | 6.2 | 8.7 | 8.9 | 21 | 5.0 | 0.5 | 12.5 | 3.6 |
| 6 | Metal Products for Architecture | 14.8 | 10.8 | 9.7 | 12 | 14.2 | 22 | 29.6 | 8.5 |
| 7 | Gas and Oil Appliances | 16.0 | 19.3 | 19.3 | 19 | 14.7 | 5.9 | 27.5 | 6.2 |
| 8 | Metal Containers | 17.2 | 19.7 | 20.8 | 72 | 17.3 | 1.4 | 33.8 | 9.0 |
| 9 | Metal Tools | 8.3 | 4.4 | 4.2 | 49 | 5.8 | 0.1 | 26.8 | 6.3 |
| 10 | Plumber Supplies | 10.5 | 13.4 | 12.1 | 20 | 9.6 | 3.8 | 21.3 | 5.9 |
| 11 | Metal Strongboxes | 15.6 | 12.6 | 11.6 | 5 | 13.0 | 5.2 | 28.0 | 8.5 |
| 12 | Boiler and Engines | 16.2 | 15.9 | 22.0 | 58 | 13.1 | 23 | 39.2 | 10.5 |
| 13 | Pumps and Compressors | 12.6 | 11.7 | 14.9 | 51 | 11.8 | 0.3 | 39.9 | 9.3 |
| 14 | Metal Machine Tools | 17.4 | 15.6 | 17.8 | 66 | 15.9 | 1.6 | 40.2 | 9.3 |
| 15 | Metal Processing Machinery | 14.3 | 23.6 | 18.5 | 113 | 123 | 0.3 | 40.3 | 9.4 |
| 16 | Machinists' Precision Tools | 16.6 | 14.9 | 17.7 | 10 | 16.5 | 6.6 | 29.4 | 6.9 |
| 17 | Industrial Robots | 10.8 | 9.9 | 12.1 | 12 | 9.6 | 3.3 | 18.3 | 5.2 |
| 18 | Construction Machinery | 11.2 | 12.6 | 14.3 | 83 | 10.8 | 0.6 | 33.4 | 7.6 |
| 19 | Food Processing Machinery | 13.1 | 19.7 | 18.9 | 78 | 11.7 | 1.3 | 36.3 | 7.9 |
| 20 | Printing and Bookbinding Machinery | 12.7 | 14.1 | 16.0 | 34 | 11.2 | 1.5 | 28.3 | 7.0 |
| 21 | Chemical Machinery | 13.8 | 22.7 | 25.4 | 155 | 120 | 0.7 | 40.9 | 9.4 |
| 22 | Semiconductor Making Equipment | 9.2 | 8.4 | 9.6 | 39 | 7.8 | 0.8 | 26.7 | 6.0 |
| 23 | Other Office Machinery | 128 | 11.7 | 14.8 | 24 | 12.1 | 4.2 | 25.8 | 5.2 |
| 24 | Machinery for Service Industry | 10.6 | 10.7 | 19.6 | 83 | 10.8 | 0.7 | 40.2 | 6.4 |
| 25 | Conveyors | 10.4 | 10.5 | 11.3 | 47 | 9.6 | 0.5 | 30.8 | 6.7 |
| 26 | Wrapping and Packing Machinery | 14.0 | 29.8 | 33.8 | 49 | 12.1 | 1.9 | 41.3 | 8.1 |
| 27 | Casting Equipment | 15.7 | 13.8 | 13.5 | 10 | 11.3 | 6.0 | 36.8 | 10.2 |
| 28 | Plastic Processing Machinery | 13.7 | 12.9 | 14.3 | 18 | 13.3 | 3.1 | 22.0 | 5.1 |
| 29 | Industrial Furnaces | 16.3 | 25.6 | 26.6 | 30 | 15.8 | 1.3 | 34.3 | 11.0 |
| 30 | Combustion Furnaces | 11.1 | 16.8 | 21.3 | 115 | 9.7 | 2.0 | 30.7 | 6.2 |
| 31 | Copy Machines | 7.9 | 7.0 | 7.6 | 39 | 7.2 | 0.6 | 15.3 | 3.2 |
| 32 | Refrigerators and Air Conditioning Apparatus | 13.6 | 10.8 | 12.6 | 72 | 12.0 | 1.9 | 33.3 | 7.8 |
| 33 | Other Industrial Heavy Electrical Equipment | 11.7 | 17.6 | 20.0 | 107 | 9.6 | 1.2 | 43.0 | 8.9 |
| 34 | Television and Video Equipment | 9.8 | 11.1 | 12.3 | 58 | 8.4 | 0.1 | 22.4 | 6.3 |
| 35 | Air Conditioners | 13.8 | 14.5 | 15.8 | 315 | 12.5 | 0.5 | 40.8 | 7.8 |
| 36 | Electric Appliances for Kitchen | 13.0 | 18.6 | 25.6 | 98 | 11.6 | 0.5 | 39.3 | 8.3 |
| 37 | Electric Ligthting Fixtures and Apparatus | 12.4 | 9.1 | 10.2 | 20 | 12.0 | 1.8 | 23.3 | 6.3 |
| 38 | Personal Computers | 7.2 | 5.4 | 6.2 | 224 | 6.3 | 0.4 | 19.3 | 3.3 |
| 39 | Mainframes and Servers | 7.4 | 6.6 | 7.6 | 134 | 6.8 | 0.1 | 21.4 | 4.3 |
| 40 | Wired Communication Equipment | 9.2 | 8.7 | 9.8 | 159 | 8.8 | 0.3 | 28.3 | 5.3 |
| 41 | Wireless Communication Equipment | 9.8 | 9.3 | 14.2 | 24 | 8.1 | 3.9 | 25.6 | 5.9 |
| 42 | Applied Electronic Equipment | 11.0 | 9.6 | 14.1 | 132 | 10.6 | 0.5 | 31.4 | 5.9 |
| 43 | Electric Measuring Instruments | 16.7 | 14.1 | 18.0 | 23 | 13.9 | 5.5 | 34.9 | 7.5 |
| 44 | Generators and Motors | 17.1 | 25.5 | 26.2 | 32 | 15.8 | 1.1 | 36.8 | 9.3 |
| 45 | Relay Switches and Switchboards | 12.5 | 15.2 | 20.7 | 22 | 12.7 | 0.8 | 35.6 | 10.4 |
| 46 | Transformers and Reactors | 14.9 | 16.3 | 19.6 | 51 | 13.7 | 0.3 | 37.6 | 9.7 |
| 47 | Batteries | 11.2 | 11.1 | 11.2 | 15 | 9.9 | 2.1 | 22.4 | 6.0 |
| 48 | Passenger Cars | 8.4 | 8.7 | 9.8 | 261 | 7.9 | 0.5 | 20.5 | 3.8 |
| 49 | Trucks | 12.1 | 10.8 | 10.9 | 54 | 12.1 | 0.6 | 20.3 | 3.6 |
| 50 | Buses | 11.7 | 15.4 | 16.1 | 31 | 12.8 | 0.7 | 22.3 | 5.3 |
| 51 | Ships | 16.6 | 21.4 | 21.6 | 43 | 14.8 | 1.9 | 49.0 | 11.6 |
| 52 | Transport Equipment for Industry Use | 15.3 | 15.4 | 16.3 | 315 | 14.8 | 0.2 | 37.5 | 7.0 |
| 53 | Photographic and Optical Instruments | 11.6 | 11.2 | 12.3 | 26 | 11.9 | 0.5 | 27.3 | 6.4 |
| 54 | Professional and Scientific Instruments | 12.2 | 11.4 | 11.7 | 41 | 11.1 | 0.5 | 41.4 | 8.4 |
| 55 | Analytical Instruments | 11.9 | 12.3 | 12.9 | 65 | 11.7 | 1.8 | 20.9 | 4.2 |
| 56 | Measuring Instruments | 11.9 | 11.7 | 12.8 | 163 | 11.6 | 0.5 | 32.6 | 6.5 |
| 57 | Testing Instruments | 12.9 | 14.9 | 15.4 | 33 | 123 | 1.3 | 29.8 | 6.5 |
| 58 | Information Recording Media | 9.3 | 8.2 | 8.5 | 15 | 9.9 | 2.3 | 16.0 | 4.6 |
| 59 | Miscellaneous Products | 9.8 | 10.2 | 11.7 | 299 | 8.0 | 0.3 | 36.1 | 7.2 |
| 60 | Residential Buildings | 19.6 | 27.1 | 28.3 | 21 | 21.0 | 3.1 | 33.0 | 10.4 |
| 61 | Storehouses | 17.3 | 25.5 | 26.2 | 82 | 14.9 | 0.8 | 40.8 | 9.3 |
| 62 | Office Buildings | 15.4 | 22.2 | 23.0 | 261 | 13.6 | 0.9 | 39.9 | 9.7 |
| 63 | Stores | 13.4 | 20.9 | 23.4 | 58 | 10.6 | 2.4 | 38.9 | 9.3 |
| 64 | Factories | 17.2 | 23.0 | 24.3 | 89 | 15.8 | 0.7 | 42.7 | 9.6 |
| 65 | Road and Parking Areas | 11.6 | 16.5 | 17.0 | 192 | 10.9 | 0.2 | 32.7 | 8.2 |
| 66 | Other Construction | 10.8 | 12.5 | 13.2 | 105 | 10.5 | 1.2 | 31.9 | 6.6 |
|  | Simple Average | 12.6 | 14.3 | 15.8 | 81.3 | 11.5 | 1.6 | 31.4 | 7.3 |

Table. 3 Estimates of the Weibull Distribution: Case-1 $\left(S_{0}(\tau)\right)$

|  |  | - | (t-value) | $\beta$ | (t-value) | $\lambda$ | $T$ | adj $\mathrm{R}^{2}$ | smpl |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 2.33 | 7.5 | -4.84 | -8.1 | 8.0 | 7.1 | 0.823 | ${ }_{1} 13$ |
| 2 | Furniture | 1.55 | 139.3 | -3.80 | -152.8 | 11.6 | 10.4 | 0.984 | 309 |
| 3 | Steel Pipes and Tubes | 1.55 | 51.9 | -4.60 | -56.3 | 19.2 | 17.3 | 0.983 | 47 |
| 4 | Electric Wires and Cables | 1.37 | 322 | -3.24 | -35.4 | 10.7 | 9.8 | 0.961 | 43 |
| 5 | Optical Fiber Cable | 1.19 | 13.2 | -2.35 | -14.5 | 7.1 | 6.7 | 0.897 | 21 |
| 6 | Metal Products for Architecture | 1.25 | 10.7 | -3.52 | -11.6 | 16.6 | 15.5 | 0.911 | 12 |
| 7 | Gas and Oil Appliances | 2.66 | 32.8 | -7.64 | -34.6 | 17.7 | 15.7 | 0.984 | 19 |
| 8 | Metal Containers | 1.68 | 62.2 | -5.00 | -67.4 | 19.5 | 17.4 | 0.982 | 72 |
| 9 | Metal Tools | 1.14 | 24.0 | -2.53 | -26.4 | 9.2 | 8.8 | 0.923 | 49 |
| 10 | Plumber Supplies | 1.87 | 15.6 | -4.58 | -16.9 | 11.6 | 10.3 | 0.928 | 20 |
| 11 | Metal Strongboxes | 1.46 | 6.9 | -4.11 | -7.4 | 16.8 | 15.2 | 0.922 | 5 |
| 12 | Boiler and Engines | 1.61 | 49.1 | -4.63 | -53.4 | 17.8 | 16.0 | 0.977 | 58 |
| 13 | Pumps and Compressors | 1.17 | 56.8 | -3.06 | -62.4 | 13.7 | 13.0 | 0.985 | 51 |
| 14 | Metal Machine Tools | 1.67 | 54.0 | -4.99 | -58.5 | 19.8 | 17.7 | 0.978 | 66 |
| 15 | Metal Processing Machinery | 1.29 | 65.4 | -3.59 | -71.8 | 16.2 | 14.9 | 0.974 | 113 |
| 16 | Machinists' Precision Tools | 2.20 | 14.1 | -6.40 | -14.9 | 18.4 | 16.3 | 0.957 | 10 |
| 17 | Industrial Robots | 1.92 | 16.6 | -4.76 | -17.8 | 11.9 | 10.6 | 0.961 | 12 |
| 18 | Construction Machinery | 1.39 | 92.7 | -3.48 | -101.7 | 124 | 11.3 | 0.991 | 83 |
| 19 | Food Processing Machinery | 1.68 | 57.9 | -4.53 | -63.0 | 14.7 | 13.2 | 0.978 | 78 |
| 20 | Printing and Bookbinding Machinery | 1.66 | 39.9 | -4.42 | -43.3 | 14.3 | 128 | 0.980 | 34 |
| 21 | Chemical Machinery | 1.36 | 122.9 | -3.71 | -134.8 | 15.3 | 14.0 | 0.990 | 155 |
| 22 | Semiconductor Making Equipment | 1.32 | 28.1 | -3.09 | -30.9 | 10.4 | 9.6 | 0.954 | 39 |
| 23 | Other Office Machinery | 2.56 | 35.3 | -6.78 | -37.5 | 14.2 | 12.6 | 0.982 | 24 |
| 24 | Machinery for Service Industry | 1.54 | 37.7 | -3.84 | -41.4 | 12.2 | 11.0 | 0.945 | 83 |
| 25 | Conveyors | 1.48 | 36.6 | -3.62 | -40.1 | 11.6 | 10.5 | 0.967 | 47 |
| 26 | Wrapping and Packing Machinery | 1.86 | 41.0 | -5.12 | -44.3 | 15.7 | 13.9 | 0.972 | 49 |
| 27 | Casting Equipment | 1.66 | 7.3 | -4.72 | -7.8 | 17.1 | 15.3 | 0.853 | 10 |
| 28 | Plastic Processing Machinery | 2.16 | 13.5 | -5.94 | -14.4 | 15.5 | 13.7 | 0.914 | 18 |
| 29 | Industrial Furnaces | 1.17 | 25.7 | -3.38 | -28.2 | 17.8 | 16.8 | 0.958 | 30 |
| 30 | Combustion Fumaces | 2.33 | 36.5 | -5.87 | -39.4 | 12.4 | 11.0 | 0.921 | 115 |
| 31 | Copy Machines | 1.94 | 14.6 | -4.31 | -15.9 | 9.2 | 8.2 | 0.847 | 39 |
| 32 | Refrigerators and Air Conditioning Apparatus | 1.80 | 97.1 | -4.91 | -105.3 | 15.2 | 13.5 | 0.993 | 72 |
| 33 | Other Industrial Heavy Electrical Equipment | 1.41 | 65.4 | -3.57 | -71.9 | 12.6 | 11.5 | 0.976 | 107 |
| 34 | Television and Video Equipment | 1.20 | 25.9 | -2.91 | -28.6 | 11.4 | 10.7 | 0.922 | 58 |
| 35 | Air Conditioners | 1.76 | 208.9 | -4.82 | -227.2 | 15.5 | 13.8 | 0.993 | 315 |
| 36 | Electric Appliances for Kitchen | 1.53 | 110.8 | -4.10 | -121.1 | 14.5 | 13.0 | 0.992 | -98 |
| 37 | Electric Ligthting Fixtures and Apparatus | 1.45 | 18.4 | -3.84 | -20.1 | 14.1 | 128 | 0.944 | 21 |
| 38 | Personal Computers | 2.60 | 53.3 | -5.45 | -57.7 | 8.1 | 7.2 | 0.927 | 224 |
| 39 | Mainframes and Servers | 1.57 | 48.6 | -3.36 | -53.6 | 8.5 | 7.7 | 0.947 | 134 |
| 40 | Wired Communication Equipment | 1.63 | 136.8 | -3.80 | -150.0 | 10.4 | 9.3 | 0.992 | 159 |
| 41 | Wireless Communication Equipment | 1.95 | 14.0 | -4.64 | -15.2 | 10.8 | 9.6 | 0.895 | 24 |
| 42 | Applied Electronic Equipment | 1.63 | 58.6 | -4.15 | -64.2 | 12.7 | 11.3 | 0.963 | 132 |
| 43 | Electric Measuring Instruments | 2.51 | 21.2 | $-7.32$ | -22.5 | 18.5 | 16.4 | 0.953 | $\underline{23}$ |
| 44 | Generators and Motors | 1.57 | 21.3 | -4.67 | -23.1 | 19.5 | 17.6 | 0.936 | 32 |
| 45 | Relay Switches and Switchboards | 0.88 | 16.7 | -2.24 | -18.3 | 12.6 | 13.4 | 0.930 | 22 |
| 47 | Transformers and Reactors Batteries | 1.13 | 34.8 | -3.19 | -38.3 | 16.9 | 16.1 | 0.960 | 51 |
| 48 | Passenger Cars | 1.62 2.17 | 15.6 | -4.10 -4.90 | -16.9 -139.3 | 12.5 9.6 | 11.2 8.5 | 0.945 0.984 | 15 |
| 49 | Trucks | 2.02 | 11.3 | -5.43 | -12.3 | 14.6 | 13.0 | 0.705 | 54 |
| 50 | Buses | 1.26 | 11.1 | -3.36 | -12.3 | 14.4 | 13.4 | 0.804 | 31 |
| 51 | Ships | 1.45 | 56.3 | -4.20 | -61.3 | 14.4 | 16.4 | 0.987 | 43 |
| 52 | Transport Equipment for Industry Use | 1.90 | 75.4 | -5.46 | -81.6 | 17.8 | 15.8 | 0.948 | 315 |
| 53 | Photographic and Optical Instruments | 1.27 | 15.3 | -3.30 | -16.8 | 13.6 | 12.6 | 0.903 | 26 |
| 54 | Professional and Scientific Instruments | 1.31 | 37.9 | -3.41 | -41.6 | 13.6 | 12.5 | 0.973 | 41 |
| 55 | Analytical Instruments | 2.53 | 29.8 | -6.60 | -31.9 | 13.5 | 120 | 0.933 | 65 |
| 56 | Measuring Instruments | 1.64 | 81.1 | -4.29 | -88.7 | 13.7 | 12.2 | 0.976 | 163 |
| 57 | Testing Instruments | 1.55 | 21.5 | -4.20 | -23.4 | 14.9 | 13.4 | 0.935 | 33 |
| 58 | Information Recording Media | 1.69 | 16.7 | -3.97 | -18.1 | 10.4 | 9.3 | 0.952 | 15 |
| 59 | Miscellaneous Products | 1.37 | 282.1 | -3.24 | -309.7 | 10.6 | 9.7 | 0,996 | 299 |
| 60 | Residential Buildings Storehouses | 1.45 1.62 | 17.4 47.4 | -4.50 -4.84 | -18.9 | 22.2 | 20.1 | 0.938 | 21 82 |
| 61 | Storehouses Office Buildings | 1.62 1.47 | 47.4 132.1 | -4.84 -4.18 | -51.5 -144.5 | 19.7 | 17.7 15.6 | 0.965 0.985 | 82 261 |
| 63 | Stores | 1.68 | 35.5 | -4.51 | -148.5 | 14.7 | 13.6 | 0.957 | 261 58 |
| 64 | Factories | 1.56 | 52.3 | -4.64 | -56.9 | 19.8 | 17.8 | 0.969 | 89 |
| 65 | Road and Parking Areas | 1.29 | 147.1 | -3.27 | -161.6 | 12.7 | 11.7 | 0.991 | 192 |
| 66 | Other Construction | 1.64 | 86.3 | -4.09 | -94.3 | 121 | 10.8 | 0.986 | 105 |

Table. 4 The Weibull Survival Rates: Case-1 $\left(S_{0}(\tau)\right)$

|  |  | 0 | 5 | 10 | 15 | 20 | 30 | $40^{\circ}$ | 50 | $\overline{60} \cdots$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 100 | 71.4 | 18.3 | 1.3 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 2 | Furniture | 100 | 76.2 | 45.1 | 22.4 | 9.6 | 1.2 | 0.1 | 0.0 | 0.0 |
| 3 | Steel Pipes and Tubes | 100 | 88.4 | 69.6 | 50.7 | 34.5 | 13.6 | 4.4 | 1.2 | 0.3 |
| 4 | Electric Wires and Cables | 100 | 70.2 | 40.1 | 20.4 | 9.5 | 1.6 | 0.2 | 0.0 | 0.0 |
| 5 | Optical Fiber Cable | 100 | 520 | 22.4 | 8.8 | 3.3 | 0.4 | 0.0 | 0.0 | 0.0 |
| 6 | Metal Products for Architecture | 100 | 80.1 | 58.9 | 41.5 | 28.3 | 12.3 | 4.9 | 1.9 | 0.7 |
| 7 | Gas and Oil Appliances | 100 | 96.6 | 80.2 | 52.3 | 24.8 | 1.7 | 0.0 | 0.0 | 0.0 |
| 8 | Metal Containers | 100 | 90.4 | 72.3 | 52.6 | 35.2 | 12.7 | 3.5 | 0.8 | 0.1 |
| 9 | Metal Tools | 100 | 60.7 | 33.4 | 17.5 | 8.9 | 2.2 | 0.5 | 0.1 | 0.0 |
| 10 | Plumber Supplies | 100 | 81.3 | 47.1 | 20.1 | 6.4 | 0.3 | 0.0 | 0.0 | 0.0 |
| 11 | Metal Strongboxes | 100 | 84.3 | 62.5 | 42.9 | 27.6 | 9.8 | 2.9 | 0.8 | 0.2 |
| 12 | Boiler and Engines | 100 | 87.8 | 67.4 | 46.9 | 30.1 | 10.0 | 2.6 | 0.5 | 0.1 |
| 13 | Pumps and Compressors | 100 | 73.5 | 50.1 | 32.9 | 21.1 | 8.2 | 3.0 | 1.1 | 0.4 |
| 14 | Metal Machine Tools | 100 | 90.4 | 72.6 | 53.2 | 36.1 | 13.4 | 3.9 | 0.9 | 0.2 |
| 15 | Metal Processing Machinery | 100 | 80.2 | 58.4 | 40.3 | 26.8 | 10.8 | 4.0 | 1.4 | 0.4 |
| 16 | Machinists' Precision Tools | 100 | 94.4 | 76.9 | 52.6 | 29.9 | 5.3 | 0.4 | 0.0 | 0.0 |
| 17 | Industrial Robots | 100 | 82.8 | 49.0 | 21.1 | 6.7 | 0.3 | 0.0 | 0.0 | 0.0 |
| 18 | Construction Machinery | 100 | 75.2 | 47.5 | 27.1 | 14.3 | 3.3 | 0.6 | 0.1 | 0.0 |
| 19 | Food Processing Machinery | 100 | 85.0 | 59.4 | 35.7 | 18.8 | 3.6 | 0.5 | 0.0 | 0.0 |
| 20 | Printing and Bookbinding Machinery | 100 | 84.1 | 57.7 | 34.0 | 17.6 | 3.3 | 0.4 | 0.0 | 0.0 |
| 21 | Chemical Machinery | 100 | 80.4 | 57.0 | 37.7 | 23.7 | 8.2 | 2.5 | 0.7 | 0.2 |
| 22 | Semiconductor Making Equipment | 100 | 68.3 | 38.6 | 19.6 | 9.2 | 1.7 | 0.3 | 0.0 | 0.0 |
| 23 | Other Office Machinery | 100 | 93.3 | 66.4 | 31.5 | 9.0 | 0.1 | 0.0 | 0.0 | 0.0 |
| 24 | Machinery for Service Industry | 100 | 77.5 | 47.7 | 25.2 | 11.7 | 1.8 | 0.2 | 0.0 | 0.0 |
| 25 | Conveyors | 100 | 75.1 | 45.0 | 23.4 | 10.8 | 1.8 | 0.2 | 0.0 | 0.0 |
| 26 | Wrapping and Packing Machinery | 100 | 88.8 | 64.8 | 39.8 | 20.7 | 3.5 | 0.3 | 0.0 | 0.0 |
| 27 | Casting Equipment | 100 | 87.8 | 66.3 | 44.6 | 27.2 | 7.8 | 1.6 | 0.3 | 0.0 |
| 28 | Plastic Processing Machinery | 100 | 91.7 | 67.9 | 39.5 | 17.7 | 1.5 | 0.0 | 0.0 | 0.0 |
| 29 | Industrial Furnaces | 100 | 79.8 | 60.1 | 44.1 | 31.7 | 15.8 | 7.5 | 3.5 | 1.6 |
| 30 | Combustion Furnaces | 100 | 88.6 | 54.5 | 21.0 | 4.7 | 0.0 | 0.0 | 0.0 | 0.0 |
| 31 | Copy Machines | 100 | 73.6 | 30.8 | 7.5 | 1.1 | 0.0 | 0.0 | 0.0 | 0.0 |
| 32 | Refrigerators and Air Conditioning Apparatus | 100 | 87.4 | 62.4 | 37.6 | 19.3 | 3.3 | 0.3 | 0.0 | 0.0 |
| 33 | Other Industrial Heavy Electrical Equipment | 100 | 76.1 | 48.5 | 27.8 | 14.7 | 3.3 | 0.6 | 0.1 | 0.0 |
| 34 | Television and Video Equipment | 100 | 68.8 | 42.5 | 24.9 | 14.0 | 4.1 | 1.1 | 0.3 | 0.1 |
| 35 | Air Conditioners | 100 | 87.3 | 63.1 | 39.1 | 21.1 | 4.2 | 0.5 | 0.0 | 0.0 |
| 36 | Electric Appliances for Kitchen | 100 | 82.2 | 56.7 | 34.8 | 19.4 | 4.7 | 0.9 | 0.1 | 0.0 |
| 37 | Electric Ligthting Fixtures and Apparatus | 100 | 80.1 | 54.5 | 33.5 | 19.0 | 5.1 | 1.1 | 0.2 | 0.0 |
| 38 | Personal Computers | 100 | 75.4 | 18.0 | 0.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 39 | Mainframes and Servers | 100 | 64.8 | 27.7 | 8.9 | 2.2 | 0.1 | 0.0 | 0.0 | 0.0 |
| 40 | Wired Communication Equipment | 100 | 73.7 | 39.0 | 16.2 | 5.5 | 0.4 | 0.0 | 0.0 | 0.0 |
| 41 | Wireless Communication Equipment | 100 | 80.1 | 42.6 | 15.2 | 3.7 | 0.1 | 0.0 | 0.0 | 0.0 |
| 42 | Applied Electronic Equipment | 100 | 80.4 | 50.7 | 26.8 | 12.2 | 1.7 | 0.1 | 0.0 | 0.0 |
| 43 | Electric Measuring Instruments | 100 | 96.3 | 80.7 | 55.3 | 29.5 | 3.4 | 0.1 | 0.0 | 0.0 |
| 44 | Generators and Motors | 100 | 88.9 | 70.5 | 51.7 | 35.5 | 14.1 | 4.6 | 1.3 | 0.3 |
| 45 | Relay Switches and Switchboards | 100 | 64.3 | 44.3 | 31.2 | 22.3 | 11.7 | 6.3 | 3.5 | 1.9 |
| 46 | Transformers and Reactors | 100 | 77.6 | 57.5 | 41.6 | 29.7 | 14.7 | 7.0 | 3.3 | 1.5 |
| 47 | Batteries | 100 | 79.7 | 49.8 | 26.0 | 11.6 | 1.6 | 0.1 | 0.0 | 0.0 |
| 48 | Passenger Cars | 100 | 78.4 | 33.4 | 7.1 | 0.7 | 0.0 | 0.0 | 0.0 | 0.0 |
| 49 | Trucks | 100 | 89.2 | 63.0 | 35.0 | 15.3 | 1.4 | 0.0 | 0.0 | 0.0 |
| 50 | Buses | 100 | 76.8 | 53.1 | 34.9 | 220 | 8.0 | 2.7 | 0.8 | 0.2 |
| 51 | Ships | 100 | 80.6 | 55.5 | 34.6 | 19.9 | 5.5 | 1.2 | 0.2 | 0.0 |
| 52 | Transport Equipment for Industry Use | 100 | 91.4 | 71.5 | 48.4 | 28.6 | 6.7 | 0.9 | 0.1 | 0.0 |
| 53 | Photographic and Optical Instruments | 100 | 75.4 | 50.7 | 32.1 | 19.5 | 6.5 | 2.0 | 0.5 | 0.1 |
| 54 | Professional and Scientific Instruments | 100 | 76.3 | 51.1 | 31.9 | 18.9 | 5.9 | 1.6 | 0.4 | 0.1 |
| 55 | Analytical Instruments | 100 | 923 | 62.8 | 27.3 | 6.8 | 0.1 | 0.0 | 0.0 | 0.0 |
| 56 | Measuring Instruments | 100 | 82.5 | 54.9 | 31.1 | 15.4 | 2.6 | 0.3 | 0.0 | 0.0 |
| 57 | Testing Instruments | 100 | 83.3 | 58.5 | 36.5 | 20.7 | 5.2 | 1.0 | 0.1 | 0.0 |
| 58 | Information Recording Media | 100 | 75.0 | 39.4 | 15.8 | 4.9 | 0.3 | 0.0 | 0.0 | 0.0 |
| 59 | Miscellaneous Products | 100 | 70.1 | 39.8 | 20.0 | 9.2 | 1.6 | 0.2 | 0.0 | 0.0 |
| 60 | Residential Buildings | 100 | 89.1 | 73.0 | 56.7 | 42.3 | 21.2 | 9.5 | 3.9 | 1.4 |
| 61 | Storehouses | 100 | 89.8 | 71.8 | 52.7 | 36.0 | 13.9 | 4.3 | 1.1 | 0.2 |
| 62 | Office Buildings | 100 | 85.0 | 63.7 | 44.1 | 28.7 | 10.4 | 3.2 | 0.8 | 0.2 |
| 63 | Stores | 100 | 84.9 | 59.2 | 35.5 | 18.7 | 3.6 | 0.5 | 0.0 | 0.0 |
| 64 | Factories | 100 | 88.9 | 70.7 | 52.1 | 36.1 | 14.7 | 5.0 | 1.4 | 0.4 |
| 65 | Road and Parking Areas | 100 | 73.9 | 47.9 | 28.9 | 16.6 | 4.9 | 1.3 | 0.3 | 0.1 |
| 66 | Other Construction | 100 | 79.0 | 48.0 | 23.9 | 10.1 | 1.1 | 0.1 | 0.0 | 0.0 |

Table. 5 Estimates of the Weibull Distribution: Case-2 $\left(S_{v}(\tau)\right)$

|  |  | a | (t-value) | $\beta$ | (t-value) | $\lambda$ | 7 | adj $\mathrm{R}^{2}$ | smpl |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 2.82 | 4.3 | -6.03 | -4.8 | 8.5 | 7.5 | 0.597 | 13 |
| 2 | Furniture | 1.62 | 77.5 | -3.88 | -83.3 | 11.0 | 9.9 | 0.951 | 309 |
| 3 | Steel Pipes and Tubes | 230 | 25.4 | -6.95 | -28.1 | 20.5 | 18.1 | 0.933 | 47 |
| 4 | Electric Wires and Cables | 293 | 12.3 | -8.44 | -16.4 | 17.8 | 15.9 | 0.781 | 43 |
| 5 | Optical Fiber Cable | 1.50 | 7.8 | -4.16 | -12.0 | 16.0 | 14.4 | 0.747 | 21 |
| 6 | Metal Products for Architecture | 1.34 | 11.6 | -3.43 | -11.5 | 13.0 | 12.0 | 0.924 | 12 |
| 7 | Gas and Oil Appliances | 3.00 | 18.5 | -9.24 | -20.8 | 21.7 | 19.3 | 0.950 | 19 |
| 8 | Metal Containers | 2.41 | 63.9 | -7.55 | -72.9 | 22.8 | 20.2 | 0.983 | 72 |
| 9 | Metal Tools | 248 | 10.3 | -5.27 | -10.9 | 8.4 | 7.5 | 0.687 | 49 |
| 10 | Plumber Supplies | 2.63 | 13.8 | -7.12 | -16.6 | 15.1 | 13.4 | 0.909 | 20 |
| 11 | Metal Strongboxes | 1.39 | 7.4 | -3.59 | -7.1 | 13.1 | 120 | 0.930 |  |
| 12 | Boiler and Engines | 2.02 | 31.9 | -5.97 | -35.5 | 19.1 | 16.9 | 0,947 | 58 |
| 13 | Pumps and Compressors | 1.56 | 23.0 | -4.19 | -25.8 | 14.6 | 13.1 | 0.913 | 51 |
| 14 | Metal Machine Tools | 2.14 | 40.9 | -6.23 | -43.2 | 18.2 | 16.2 | 0.963 | 66 |
| 15 | Metal Processing Machinery | 1.65 | 44.7 | -5.49 | -58.8 | 27.8 | 24.9 | 0.947 | 113 |
| 16 | Machinists' Precision Tools | 2.21 | 6.9 | -6.27 | -7.1 | 17.0 | 15.1 | 0.838 | 10 |
| 17 | Industrial Robots | 1.06 | 8.9 | -267 | -9.7 | 12.5 | 12.2 | 0.876 | 12 |
| 18 | Construction Machinery | 1.89 | 50.3 | -5.08 | -59.0 | 14.7 | 13.0 | 0.969 | 83 |
| 19 | Food Processing Machinery | 2.03 | 27.6 | -6.85 | -37.7 | 29.3 | 26.0 | 0.908 | 78 |
| 20 | Printing and Bookbinding Machinery | 3.33 | 14.8 | -9.25 | -16.7 | 16.1 | 14.4 | 0.868 | 34 |
| 21 | Chemical Machinery | 1.92 | 71.9 | -6.48 | -97.5 | 29.1 | 25.8 | 0.971 | 155 |
| 22 | Semiconductor Making Equipment | 247 | 28.8 | -5.56 | -30.4 | 9.5 | 8.4 | 0.956 | 39 |
| 23 | Other Office Machinery | 3.26 | 20.2 | -8.42 | -20.9 | 13.3 | 11.9 | 0.946 | 24 |
| 24 | Machinery for Service Industry | 272 | 321 | -7.01 | -36.4 | 13.1 | 11.7 | 0.926 | 83 |
| 25 | Conveyors | 2.23 | 18.4 | -5.64 | -20.8 | 12.5 | 11.0 | 0.881 | 47 |
| 26 | Wrapping and Packing Machinery | 2.27 | 19.0 | -7.46 | -24.6 | 26.7 | 23.6 | 0.883 | 49 |
| 27 | Casting Equipment | 226 | 3.8 | -6.68 | -4.2 | 19.1 | 16.9 | 0.600 | 10 |
| 28 | Plastic Processing Machinery | 245 | 12.2 | -6.66 | -129 | 15.1 | 13.4 | 0.897 | 18 |
| 29 | Industrial Furnaces | 1.61 | 14.0 | -5.79 | -19.1 | 36.2 | 32.4 | 0.870 | 30 |
| 30 | Combustion Furnaces | 228 | 26.0 | -6.42 | -31.4 | 16.7 | 14.8 | 0.856 | 115 |
| 31 | Copy Machines | 1.80 | 14.0 | -3.89 | -14.9 | 8.7 | 7.7 | 0.837 | 39 |
| 32 | Refrigerators and Air Conditioning Apparatus | 2.18 | 13.7 | -5.80 | -14.5 | 14.3 | 12.7 | 0.724 | 72 |
| 33 | Other Industrial Heavy Electrical Equipment | 1.60 | 42.5 | -4.84 | -55.5 | 20.4 | 18.3 | 0.944 | 107 |
| 34 | Television and Video Equipment | 1.05 | 16.4 | -2.94 | -21.0 | 16.6 | 16.4 | 0.825 | 58 |
| 35 | Air Conditioners | 1.88 | 129.9 | -5.25 | -143.4 | 16.2 | 14.4 | 0.982 | 315 |
| 36 | Electric Appliances for Kitchen | 1.53 | 45.2 | -4.66 | -56.5 | 21.2 | 19.1 | 0.955 | 315 98 |
| 37 | Electric Ligthting Fixtures and Apparatus | 0.88 | 11.4 | -201 | -13.7 | 9.9 | 10.6 | 0.865 | 21 |
| 38 39 | Personal Computers | 265 | 27.7 | -4.97 | -26.9 | 6.5 | 5.8 | 0.775 | 224 |
| 39 | Mainframes and Servers | 1.83 | 44.2 | -3.70 | -45.9 | 7.5 | 6.7 | 0.936 | 134 |
| 40 | Wired Communication Equipment | 261 | 80.2 | -6.15 | -88.4 | 10.5 | 9.4 | 0.976 | 159 |
| 41 | Wireless Communication Equipment | 1.65 | 10.5 | -3.95 | -11.5 | 11.1 | 9.9 | 0.826 | 24 |
| 42 | Applied Electronic Equipment | 1.78 | 43.4 | -4.31 | -45.4 | 11.3 | 10.1 | 0.935 | 132 |
| 43 | Electric Measuring Instruments | 3.82 | 9.0 | -11.04 | -9.4 | 18.0 | 16.3 | 0.784 | 23 |
| 44 | Generators and Motors | 3.15 | 13.2 | -11.24 | -17.1 | 35.3 | 31.6 | 0.847 | 32 |
| 45 46 | Relay Switches and Switchboards | 1.44 | 22.0 | -4.06 | -26.7 | 16.9 | 15.3 | 0.958 | 22 |
| 46 | Transformers and Reactors | 1.60 | 20.2 | -4.78 | -23.4 | 19.8 | 17.8 | 0.890 | 51 |
| 47 | Batteries | 2.03 | 9.6 | -5.07 | -10.3 | 12.2 | 10.8 | 0.867 | 15 |
| 48 | Passenger Cars | 2.32 | 1022 | -5.35 | -113.1 | 10.0 | 8.8 | 0.976 | 261 |
| 49 50 | Trucks | 240 | 15.0 | -6.01 | -15.2 | 12.2 | 10.8 | 0.809 | 54 |
| 50 | Buses Ships | 2.38 3.27 | 11.1 26.7 | -7.31 -11.06 | -14.2 | 21.5 | 19.0 26.5 | 0.803 | 31 |
| 52 | Transport Equipment for Industry Use | 1.92 | 26.7 76.2 | -11.06 -5.53 | -34.0 | 21.5 17.9 | 26.5 15.9 | 0.944 0.949 | 43 |
| 53 | Photographic and Optical Instruments | 0.92 | 76.2 9.5 | -2.46 | -10.7 | 14.5 | 15.9 15.1 | 0.949 0.780 | 215 |
| 54 | Professional and Scientific Instruments | 2.35 | 20.7 | -6.36 | -23.6 | 15.0 | 13.3 | 0.914 | 41 |
| 55 | Analytical Instruments | 230 | 27.4 | -6.12 | -29.9 | 14.3 | 127 | 0.921 | 65 |
| 56 | Measuring Instruments | 1.92 | 73.3 | -5.02 | . 80.4 | 13.8 | 12. | 0.971 | 163 |
| 57 | Testing Instruments | 246 | 10.9 | -7.46 | -13.4 | 20.8 | 18.5 | 0.787 | 33 |
| 58 59 | Information Recording Media | 1.59 | 5.7 | -3.75 | -6.3 | 10.6 | 9.5 | 0.696 | 15 |
| 59 | Miscellaneous Products | 1.72 | 120.0 | -4.17 | -135.6 | 11.4 | 10.1 | 0.980 | 299 |
| 60 | Residential Buildings | 2.64 | 15.4 | -9.16 | -18.7 | 32.1 | 28.5 | 0.922 | 21 |
| 61 | Storehouses Office Buildings | 1.70 1.80 | 22.4 | -6.33 | -30.3 | 41.2 | 36.8 | 0.861 | 82 |
| 63 | Stores | 1.80 1.66 | 52.0 33.2 | -5.90 -5.21 | -65.5 | 26.5 23.3 | 23.5 20.8 | 0.912 | 261 |
| 64 | Factories | 1.70 | 31.2 | -5.73 | -38.4 | 23.3 29.3 | 26.8 26.1 | 0.951 | 58 89 |
| 65 | Road and Parking Areas | 1.30 | 41.7 | -3.91 | -54.1 | 20.2 | 18.7 | 0.901 | 192 |
| 66 | Other Construction | 251 | 25.4 | -6.92 | -30.8 | 15.8 | 14.0 | 0.861 | 105 |

Table. 6 The Weibull Survival Rates: Case- $2\left(S_{v}(\tau)\right)$

|  |  | 0 | 5 | 10 | 15 | 20 | 30 | 40 | 50 | 60 |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 100 | 79.8 | 20.3 | 0.7 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 2 | Furniture | 100 | 75.7 | 42.6 | 19.4 | 7.3 | 0.6 | 0.0 | 0.0 | 0.0 |
| 3 | Steel Pipes and Tubes | 100 | 96.2 | 825 | 61.3 | 38.7 | 8.9 | 0.9 | 0.0 | 0.0 |
| 4 | Electric Wires and Cables | 100 | 97.6 | 83.2 | 54.7 | 24.7 | 1.0 | 0.0 | 0.0 | 0.0 |
| 5 | Optical Fiber Cable | 100 | 84.0 | 61.0 | 40.4 | 24.7 | 7.7 | 1.9 | 0.4 | 0.1 |
| 6 | Metal Products for Architecture | 100 | 75.8 | 49.6 | 29.9 | 17.0 | 4.7 | 1.1 | 0.2 | 0.0 |
| 7 | Gas and Oil Appliances | 100 | 98.8 | 90.6 | 71.7 | 45.5 | 7.0 | 0.2 | 0.0 | 0.0 |
| 8 | Metal Containers | 100 | 97.5 | 87.2 | 69.4 | 48.2 | 14.3 | 2.0 | 0.1 | 0.0 |
| 9 | Metal Tools | 100 | 75.9 | 21.5 | 1.5 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 10 | Plumber Supplies | 100 | 94.6 | 71.2 | 37.3 | 12.2 | 0.2 | 0.0 | 0.0 | 0.0 |
| 11 | Metal Strongboxes | 100 | 77.1 | 50.5 | 30.1 | 16.6 | 4.3 | 0.9 | 0.2 | 0.0 |
| 12 | Boiler and Engines | 100 | 93.6 | 76.3 | 54.2 | 33.4 | 8.3 | 1.2 | 0.1 | 0.0 |
| 13 | Pumps and Compressors | 100 | 82.9 | 57.4 | 35.1 | 19.4 | 4.5 | 0.8 | 0.1 | 0.0 |
| 14 | Metal Machine Tools | 100 | 94.0 | 75.9 | 51.8 | 29.6 | 5.5 | 0.5 | 0.0 | 0.0 |
| 15 | Metal Processing Machinery | 100 | 94.3 | 83.2 | 69.8 | 56.1 | 32.3 | 16.2 | 7.2 | 2.9 |
| 16 | Machinists' Precision Tools | 100 | 93.6 | 73.5 | 46.9 | 23.9 | 3.0 | 0.1 | 0.0 | 0.0 |
| 17 | Industrial Robots | 100 | 68.4 | 45.4 | 29.7 | 19.3 | 8.0 | 3.3 | 1.3 | 0.5 |
| 18 | Construction Machinery | 100 | 87.7 | 61.5 | 35.2 | 16.5 | 2.1 | 0.1 | 0.0 | 0.0 |
| 19 | Food Processing Machinery | 100 | 97.3 | 89.3 | 77.4 | 63.1 | 35.1 | 15.3 | 5.2 | 1.4 |
| 20 | Printing and Bookbinding Machinery | 100 | 98.0 | 81.4 | 45.2 | 126 | 0.0 | 0.0 | 0.0 | 0.0 |
| 21 | Chemical Machinery | 100 | 96.7 | 87.9 | 75.6 | 61.4 | 34.6 | 15.8 | 5.9 | 1.8 |
| 22 | Semiconductor Making Equipment | 100 | 81.4 | 320 | 4.5 | 0.2 | 0.0 | 0.0 | 0.0 | 1.8 0.0 |
| 23 | Other Office Machinery | 100 | 95.9 | 67.3 | 22.6 | 2.3 | 0.0 | 0.0 | 0.0 | 0.0 |
| 24 | Machinery for Service Industry | 100 | 93.1 | 62.2 | 23.8 | 4.3 | 0.0 | 0.0 | 0.0 | 0.0 |
| 25 | Conveyors | 100 | 87.8 | 54.3 | 22.0 | 5.6 | 0.1 | 0.0 | 0.0 | 0.0 |
| 26 | Wrapping and Packing Machinery | 100 | 97.8 | 89.8 | 76.3 | 59.4 | 27.1 | 8.1 | 1.5 | 0.2 |
| 27 | Casting Equipment | 100 | 95.3 | 79.4 | 56.1 | 33.1 | 6.3 | 0.5 | 0.0 | 0.0 |
| 28 | Plastic Processing Machinery | 100 | 93.6 | 69.7 | 37.6 | 13.8 | 0.5 | 0.0 | 0.0 | 0.0 |
| 29 | Industrial Furnaces | 100 | 96.0 | 88.2 | 78.5 | 68.1 | 47.7 | 30.9 | 18.5 | 10.4 |
| 30 | Combustion Furnaces | 100 | 93.8 | 73.2 | 45.5 | 21.9 | 2.2 | 0.1 | 0.0 | 10.4 0.0 |
| 31 | Copy Machines | 100 | 69.1 | 27.6 | 6.9 | 1.1 | 0.0 | 0.0 | 0.0 | 0.0 |
| 32 | Refrigetators and Air Conditioning Apparatus | 100 | 90.4 | 63.4 | 33.2 | 127 | 0.7 | 0.0 | 0.0 | 0.0 |
| 33 | Other Industrial Heavy Electrical Equipment | 100 | 90.0 | 72.7 | 54.3 | 37.9 | 15.6 | 5.3 | 1.5 | 0.4 |
| 34 | Television and Video Equipment | 100 | 75.2 | 55.6 | 40.8 | 29.8 | 15.7 | 8.2 | 4.3 | 2.2 |
| 35 | Air Conditioners | 100 | 89.7 | 66.9 | 42.1 | 22.6 | 4.1 | 0.4 | 0.0 | 0.0 |
| 36 | Electric Appliances for Kitchen | 100 | 89.6 | 72.8 | 55.4 | 40.0 | 18.3 | 7.1 | 2.4 | 0.7 |
| 37 | Electric Ligthting Fixtures and Apparatus | 100 | 57.8 | 36.6 | 23.8 | 15.8 | 7.2 | 3.4 | 1.6 | 0.8 |
| 38 | Personal Computers | 100 | 61.1 | 4.6 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 39 | Mainframes and Servers | 100 | 62.4 | 18.7 | 2.9 | 0.3 | 0.0 | 0.0 | 0.0 | 0.0 |
| 40 | Wired Communication Equipment | 100 | 86.7 | 41.7 | 8.0 | 0.5 | 0.0 | 0.0 | 0.0 | 0.0 |
| 41 | Wireless Communication Equipment | 100 | 76.3 | 42.8 | 19.2 | 7.0 | 0.6 | 0.0 | 0.0 | 0.0 |
| 42 | Applied Electronic Equipment | 100 | 79.0 | 44.7 | 19.1 | 6.3 | 0.3 | 0.0 | 0.0 | 0.0 |
| 43 | Electric Measuring Instruments | 100 | 99.3 | 90.0 | 61.0 | 22.7 | 0.1 | 0.0 | 0.0 | 0.0 |
| 44 | Generators and Motors | 100 | 99.8 | 98.1 | 93.5 | 84.7 | 55.0 | 22.7 | 5.0 | 0.5 |
| 45 | Relay Switches and Switchboards | 100 | 84.0 | 62.5 | 43.1 | 28.0 | 10.2 | 3.2 | 0.9 | 0.2 |
| 46 | Transformers and Reactors | 100 | 89.5 | 71.5 | 52.7 | 36.2 | 14.3 | 4.6 | 1.2 | 0.3 |
| 47 | Batteries | 100 | 84.9 | 51.3 | 21.9 | 6.6 | 0.2 | 0.0 | 0.0 | 0.0 |
| 48 | Passenger Cars | 100 | 81.8 | 36.7 | 7.6 | 0.7 | 0.0 | 0.0 | 0.0 | 0.0 |
| 49 | Trucks | 100 | 88.9 | 53.9 | 19.4 | 3.8 | 0.0 | 0.0 | 0.0 | 0.0 |
| 50 | Buses | 100 | 97.0 | 85.1 | 65.4 | 43.0 | 10.9 | 1.2 | 0.1 | 0.0 |
| 51 | Ships | 100 | 99.1 | 92.1 | 73.4 | 45.3 | 5.1 | 0.0 | 0.0 | 0.0 |
| 52 | Transport Equipment for Industry Use | 100 | 91.7 | 72.1 | 49.0 | 29.0 | 6.8 | 0.9 | 0.1 | 0.0 |
| 53 | Photographic and Optical Instruments | 100 | 68.7 | 49.1 | 35.6 | 26.1 | 14.2 | 7.8 | 4.4 | 2.5 |
| 54 | Professional and Scientific Instruments | 100 | 92.7 | 68.0 | 36.7 | 14.0 | 0.6 | 0.0 | 0.0 | 0.0 |
| 55 | Analytical Instruments | 100 | 91.5 | 64.4 | 32.7 | 11.4 | 0.4 | 0.0 | 0.0 | 0.0 |
| 56 | Measuring Instruments | 100 | 86.6 | 58.2 | 30.9 | 13.0 | 1.2 | 0.0 | 0.0 | 0.0 |
| 57 | Testing Instruments | 100 | 97.0 | 84.8 | 64.0 | 40.5 | 8.6 | 0.7 | 0.0 | 0.0 |
| 58 | Information Recording Media | 100 | 73.8 | 40.0 | 17.5 | 6.4 | 0.5 | 0.0 | 0.0 | 0.0 |
| 59 | Miscellaneous Products | 100 | 78.3 | 44.8 | 19.9 | 7.1 | 0.5 | 0.0 | 0.0 | 0.0 |
| 60 | Residential Buildings | 100 | 99.3 | 95.5 | 87.4 | 75.0 | 43.3 | 16.7 | 4.0 | 0.5 |
| 61 | Storehouses | 100 | 97.3 | 91.4 | 83.6 | 74.7 | 55.9 | 38.7 | 25.0 | 15.1 |
| 62 | Office Buildings | 100 | 95.2 | 84.1 | 69.8 | 54.7 | 28.5 | 12.2 | 4.3 | 1.3 |
| 63 | Stores | 100 | 92.5 | 78.1 | 61.7 | 45.9 | 21.8 | 8.6 | 2.9 | 0.8 |
| 64 | Factories | 100 | 95.1 | 85.1 | 72.5 | 59.2 | 35.3 | 18.3 | 8.4 | 3.4 |
| 65 | Road and Parking Areas | 100 | 85.0 | 67.0 | 50.7 | 37.3 | 18.8 | 8.8 | 3.9 | 1.6 |
| 66 | Other Construction | 100 | 94.6 | 72.7 | 41.5 | 16.4 | 0.7 | 0.0 | 0.0 | 0.0 |

Table. 7 Estimates of the Weibull Distribution: Case-3 $\left(S_{\overline{0}}(\tau)\right)$

|  |  | a | (t-value) | $\beta$ | (t-value) | $\lambda$ | T | adj $\mathbf{R}^{2}$ | smpl |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 276 | 4.3 | -5.87 | -4.7 | 8.4 | 7.5 | 0.592 | 13 |
| 2 | Furniture | 1.43 | 70.5 | -3.46 | -76.4 | 11.2 | 10.2 | 0.942 | 309 |
| 3 | Steel Pipes and Tubes | 1.92 | 27.2 | -5.83 | -30.4 | 21.0 | 18.6 | 0.941 | 47 |
| 4 | Electric Wires and Cables | 2.67 | 12.3 | -7.63 | -16.3 | 17.4 | 15.5 | 0.781 | 43 |
| 5 | Optical Fiber Cable | 1.70 | 7.8 | -4.75 | -12.2 | 16.4 | 14.6 | 0.749 | 21 |
| 6 | Metal Products for Architecture | 1.19 | 11.3 | -297 | -10.9 | 12.1 | 11.4 | 0.920 | 12 |
| 7 | Gas and Oil Appliances | 3.24 | 18.4 | -9.95 | -20.7 | 21.6 | 19.3 | 0.949 | 19 |
| 8 | Metal Containers | 2.12 | 61.6 | -6.78 | -71.9 | 24.6 | 21.8 | 0.982 | 72 |
| 9 | Metal Tools | 2.46 | 10.3 | -5.17 | -10.7 | 8.2 | 7.3 | 0.687 | 49 |
| 10 | Plumber Supplies | 2.46 | 12.6 | -6.46 | -14.6 | 13.8 | 12.2 | 0.893 | 20 |
| 11 | Metal Strong boxes | 1.21 | 6.9 | -3.00 | -6.5 | 11.9 | 11.2 | 0.922 | 5 |
| 12 | Boiler and Engines | 2.14 | 35.9 | -6.86 | -43.5 | 24.8 | 220 | 0.958 | 58 |
| 13 | Pumps and Compressors | 1.48 | 24.5 | -4.23 | -29.5 | 17.6 | 15.9 | 0.923 | 51 |
| 14 | Metal Machine Tools | 2.12 | 40.0 | -6.41 | -44.1 | 20.7 | 18.4 | 0.961 | 66 |
| 15 | Metal Processing Machinery | 1.61 | 36.6 | -4.99 | -45.7 | 22.2 | 19.9 | 0.925 | 109 |
| 16 | Machinists' Precision Tools | 2.55 | 6.5 | -7.69 | -7.1 | 20.4 | 18.1 | 0.820 | 10 |
| 17 | Industrial Robots | 1.08 | 7.3 | -3.11 | -9.1 | 17.8 | 17.3 | 0.828 | 12 |
| 18 | Construction Machinery | 1.82 | 47.9 | -5.15 | -59.1 | 16.9 | 15.0 | 0.965 | 83 |
| 19 | Food Processing Machinery | 1.72 | 27.4 | -5.72 | -37.0 | 27.9 | 24.9 | 0.907 | 78 |
| 20 | Printing and Bookbinding Machinery | 3.24 | 14.7 | -9.26 | -17.1 | 17.4 | 15.6 | 0.866 | 34 |
| 21 | Chemical Machinery | 1.91 | 76.3 | -6.70 | -107.5 | 33.1 | 29.4 | 0.974 | 155 |
| 22 | Semiconductor Making Equipment | 250 | 32.3 | -5.90 | -35.8 | 10.6 | 29.4 9.4 | 0.965 | - 39 |
| 23 | Other Office Machinery | 3.06 | 20.1 | -8.47 | -22.3 | 15.9 | 14.2 | 0.946 | 24 |
| 24 | Machinery for Service Industry | 274 | 33.8 | -8.07 | -43.7 | 19.1 | 17.0 | 0.933 | 83 |
| 25 | Conveyors | 2.11 | 18.7 | -5.42 | -21.4 | 13.0 | 11.5 | 0.883 | 47 |
| 26 | Wrapping and Packing Machinery | 2.37 | 19.2 | -8.22 | -26.2 | 32.3 | 28.6 | 0.885 | 49 |
| 27 | Casting Equipment | 1.9 | 4.0 | -5.72 | -4.4 | 18.4 | 16.3 | 0.625 | 10 |
| 28 | Plastic Processing Machinery | 240 | 10.8 | -6.82 | -11.9 | 17.1 | 15.1 | 0.872 | 18 |
| 29 | Industrial Furnaces | 1.81 | 12.9 | -6.65 | -18.0 | 39.1 | 34.8 | 0.851 | 30 |
| 30 | Combustion Furnaces | 2.40 | 27.3 | -7.49 | -36.4 | 22.5 | 20.0 | 0.867 | 115 |
| 31 | Copy Machines | 1.82 | 14.9 | -4.05 | -16.3 | 9.2 | 8.2 | 0.853 | 39 |
| 32 | Refrigerators and Air Conditioning Apparatus | 2.29 | 13.9 | -6.28 | -15.1 | 15.4 | 13.7 | 0.730 | 72 |
| 33 | Other Industrial Heavy Electrical Equipment | 1.66 | 42.4 | -5.30 | -58.9 | 24.6 | 22.0 | 0.944 | 107 |
| 34 | Television and Video Equipment | 1.28 | 15.9 | -3.79 | -21.3 | 19.2 | 17.8 | 0.815 | 58 |
| 35 | Air Conditioners | 1.87 | 106.6 | -5.33 | -120.2 | 17.2 | 15.3 | 0.973 | 315 |
| 36 | Electric Appliances for Kitchen | 1.53 | 43.1 | -5.32 | -61.4 | 32.6 | 29.3 | 0.950 | 98 |
| 37 | Electric Ligthting Fixtures and Apparatus | 0.88 | 10.0 | -2.17 | -14.7 | 11.8 | 125 | 0.833 | 21 |
| 38 | Personal Computers | 2.76 | 28.4 | -5.49 | -29.2 | 7.3 | 6.5 | 0.783 | 224 |
| 39 | Mainframes and Servers | 1.88 | 44.2 | -4.04 | -49.0 | 8.6 | 7.7 | 0.936 | 134 |
| 40 | Wired Communication Equipment | 282 | 69.0 | -6.99 | -80.0 | 11.9 | 10.6 | 0.968 | 159 |
| 41 | Wireless Communication Equipment | 2.14 | 12.9 | -6.10 | -16.7 | 17.2 | 15.3 | 0.879 | 24 |
| 42 | Applied Electronic Equipment | 1.74 | 40.1 | -4.71 | -46.9 | 15.1 | 13.4 | 0.925 | 132 |
| 43 | Electric Measuring Instruments | 3.85 | 9.0 | -11.63 | -9.9 | 20.5 | 18.5 | 0.785 | 23 |
| 44 | Generators and Motors | 3.44 | 13.0 | -12.46 | -17.2 | 37.3 | 33.5 | 0.844 | 32 |
| 45 | Relay Switches and Switchboards | 1.46 | 21.1 | -4.70 | -29.3 | 25.3 | 22.9 | 0.955 | 22 |
| 46 | Transformers and Reactors | 1.63 | 20.0 | -5.27 | -25.2 | 25.4 | 22.7 | 0.888 | 51 |
| 47 | Batteries | 2.20 | 9.6 | -5.53 | -10.3 | 12.3 | 10.9 | 0.867 | 15 |
| 48 | Passenger Cars | 2.32 | 99.2 | -5.67 | -116.6 | 11.5 | 10.2 | 0.974 | 261 |
| 49 | Trucks | 2.20 | 14.4 | -5.54 | -14.7 | 12.4 | 11.0 | 0.797 | 261 54 |
| 50 | Buses | 2.28 | 11.2 | -7.13 | -14.6 | 23.0 | 20.3 | 0.806 | 31 |
| 51 | Ships | 3.02 | 27.0 | -10.29 | -34.6 | 23.0 | 26.8 | 0.945 | 43 |
| 52 | Transport Equipment for Industry Use | 1.64 | 87.4 | -4.98 | -97.0 | 20.7 | 18.5 | 0.961 | 315 |
| 53 | Photographic and Optical Instruments | 0.93 | 9.1 | -2.64 | -11.8 | 17.1 | 17.7 | 0.764 | 26 |
| 54 | Professional and Scientific Instruments | 1.94 | 20.6 | -5.30 | -23.7 | 15.3 | 13.6 | 0.914 | 41 |
| 55 | Analytical Instruments | 2.29 | 27.0 | -6.25 | -30.2 | 15.2 | 13.5 | 0.919 | 65 |
| 56 | Measuring Instruments | 1.90 | 67.9 | $-5.20$ | -81.7 | 15.4 | 13.7 | 0.966 | 163 |
| 57 | Testing Instruments | 2.50 | 10.7 | -7.75 | -13.4 | 22.1 | 19.6 | 0.780 | 33 |
| 58 | Information Recording Media | 1.65 | 6.0 | -3.93 | -6.6 | 10.8 | 9.7 | 0.712 | 15 |
| 59 | Miscellaneous Products | 1.74 | 1225 | -4.41 | -144.7 | 12.7 | 11.3 | 0.981 | 299 |
| 60 | Residential Buildings | 276 | 15.4 | -9.78 | -19.0 | 34.7 | 30.9 | 0.921 | 21 |
| 61 | Storehouses | 1.72 | 21.2 | -6.53 | -29.3 | 44.8 | 39.9 | 0.847 | 82 |
| 62 | Office Buildings Stores | 1.81 | 49.3 | -6.03 | -63.2 | 28.0 | 24.9 | 0.903 | 261 |
| 64 | Stores Factories | 1.61 1.69 | 28.1 29.2 | -5.28 -5.90 | -37.4 -37.3 | 26.7 32.9 | 23.9 29.4 | 0.933 0.907 | 58 89 |
| 65 | Road and Parking Areas | 1.28 | 40.0 | -5.90 -3.92 | -57.3 -52.9 | 32.9 21.3 | 29.4 19.8 | 0.907 0.893 | 89 192 |
| 66 | Other Construction | 250 | 23.9 | -7.15 | -30.1 | 17.5 | 15.5 | 0.846 | 105 |

Table. 8 The Weibull Survival Rates: Case- $3\left(S_{⿹}(\tau)\right.$ )

|  |  | 0 | 5 | 10 | 15 | 20 | 30 | 40 | 50 | $60^{-}$ |
| :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: | :---: |
| 1 | Wood Products | 100 | 78.8 | 19.9 | 0.7 | 0.0 | 0.0 | 0.0 | 0.0 | $\overline{0.0}{ }^{-}$ |
| 2 | Furniture | 100 | 73.0 | 42.8 | 22.0 | 10.2 | 1.7 | 0.2 | 0.0 | 0.0 |
| 3 | Stecl Pipes and Tubes | 100 | 93.8 | 78.5 | 59.1 | 40.1 | 13.7 | 3.2 | 0.5 | 0.1 |
| 4 | Electric Wires and Cables | 100 | 96.5 | 79.7 | 51.3 | 23.7 | 1.4 | 0.0 | 0.0 | 0.0 |
| 5 | Optical Fiber Cable | 100 | 87.6 | 65.0 | 42.4 | 24.7 | 6.2 | 1.1 | 0.1 | 0.0 |
| 6 | Metal Products for Architecture | 100 | 70.5 | 45.1 | 27.5 | 16.2 | 5.3 | 1.6 | 0.4 | 0.1 |
| 7 | Gas and Oil Appliances | 100 | 99.1 | 92.0 | 73.5 | 45.7 | 5.4 | 0.1 | 0.0 | 0.0 |
| 8 | Metal Containers | 100 | 96.6 | 86.2 | 70.4 | 524 | 21.8 | 6.1 | 1.1 | 0.1 |
| 9 | Metal Tools | 100 | 74.2 | 19.3 | 1.2 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 10 | Plumber Supplies | 100 | 92.1 | 63.6 | 29.4 | 8.3 | 0.1 | 0.0 | 0.0 | 0.0 |
| 11 | Metal Strongboxes | 100 | 70.5 | 44.6 | 26.7 | 15.4 | 4.7 | 1.3 | 0.3 | 0.1 |
| 12 | Boiler and Engines | 100 | 96.8 | 86.6 | 71.1 | 53.2 | 22.3 | 6.2 | 1.1 | 0.1 |
| 13 | Pumps and Compressors | 100 | 85.6 | 64.8 | 45.5 | 30.0 | 11.2 | 3.5 | 0.9 | 0.2 |
| 14 | Metal Machine Tools | 100 | 95.2 | 80.8 | 60.4 | 39.6 | 11.3 | 1.8 | 0.2 | 0.0 |
| 15 | Metal Processing Machinery | 100 | 91.4 | 75.9 | 58.9 | 43.1 | 19.8 | 7.6 | 2.5 | 0.7 |
| 16 | Machinists' Precision Tools | 100 | 97.3 | 85.1 | 63.4 | 38.7 | 6.9 | 0.4 | 0.0 | 0.0 |
| 17 | Industrial Robots | 100 | 77.6 | 58.5 | 43.6 | 32.2 | 17.3 | 9.1 | 4.8 | 2.5 |
| 18 | Construction Machinery | 100 | 89.7 | 68.1 | 44.7 | 25.7 | 5.8 | 0.8 | 0.1 | 0.0 |
| 19 | Food Processing Machinery | 100 | 94.9 | 84.2 | 70.9 | 56.9 | 32.2 | 15.6 | 6.6 | 2.4 |
| 20 | Printing and Bookbinding Machinery | 100 | 98.3 | 84.8 | 54.1 | 21.0 | 0.3 | 0.0 | 0.0 | 0.0 |
| 21 | Chemical Machinery | 100 | 97.4 | 90.4 | 80.3 | 68.3 | 43.8 | 23.9 | 11.1 | 4.4 |
| 22 | Semiconductor Making Equipment | 100 | 85.8 | 42.1 | 9.2 | 0.8 | 0.0 | 0.0 | 0.0 | 0.0 |
| 23 | Other Office Machinery | 100 | 97.1 | 78.5 | 43.4 | 13.4 | 0.1 | 0.0 | 0.0 | 0.0 |
| 24 | Machinery for Service Industry | 100 | 97.5 | 84.3 | 59.6 | 32.1 | 3.2 | 0.1 | 0.0 | 0.0 |
| 25 | Conveyors | 100 | 87.6 | 56.4 | 26.0 | 8.4 | 0.3 | 0.0 | 0.0 | 0.0 |
| 26 | Wrapping and Packing Machinery | 100 | 98.8 | 93.9 | 84.9 | 72.4 | 43.1 | 18.9 | 6.0 | 1.3 |
| 27 | Casting Equipment | 100 | 92.5 | 73.9 | 51.2 | 30.8 | 7.3 | 1.0 | 0.1 | 0.0 |
| 28 | Plastic Processing Machinery | 100 | 94.9 | 75.8 | 48.0 | 23.1 | 2.0 | 0.0 | 0.0 | 0.0 |
| 29 | Industrial Furnaces | 100 | 97.6 | 91.9 | 83.9 | 74.4 | 53.9 | 35.3 | 21.0 | 11.4 |
| 30 | Combustion Furnaces | 100 | 97.4 | 86.8 | 68.7 | 47.3 | 13.7 | 1.9 | 0.1 | 0.0 |
| 31 | Copy Machines | 100 | 72.1 | 31.3 | 8.8 | 1.6 | 0.0 | 0.0 | 0.0 | 0.0 |
| 32 | Refrigerators and Air Conditioning Apparatus | 100 | 92.7 | 69.1 | 39.2 | 16.3 | 1.0 | 0.0 | 0.0 | 0.0 |
| 33 | Other Industrial Heavy Electrical Equipment | 100 | 93.1 | 79.8 | 64.4 | 49.2 | 25.0 | 10.7 | 4.0 | 1.3 |
| 34 | Television and Video Equipment | 100 | 83.7 | 64.9 | 48.3 | 34.9 | 17.0 | 7.7 | 3.3 | 1.3 |
| 35 | Air Conditioners | 100 | 90.6 | 69.7 | 46.3 | 26.7 | 6.0 | 0.8 | 0.1 | 0.0 |
| 36 | Electric Appliances for Kitchen | 100 | 94.5 | 84.8 | 73.6 | 62.2 | 41.4 | 25.4 | 14.6 | 7.8 |
| 37 | Electric Ligthting Fixtures and Apparatus | 100 | 624 | 42.0 | 29.0 | 20.3 | 10.3 | 5.3 | 2.8 | 1.5 |
| 38 | Personal Computers | 100 | 70.4 | 9.3 | 0.1 | 0.0 | 0.0 | 0.0 | 0.0 | 0.0 |
| 39 | Mainframes and Servers | 100 | 69.8 | 26.7 | 6.0 | 0.8 | 0.0 | 0.0 | 0.0 | 0.0 |
| 40 | Wired Communication Equipment | 100 | 91.7 | 54.2 | 14.6 | 1.3 | 0.0 | 0.0 | 0.0 | 0.0 |
| 41 | Wireless Communication Equipment | 100 | 93.2 | 73.2 | 47.6 | 25.3 | 3.8 | 0.2 | 0.0 | 0.0 |
| 42 | Applied Electronic Equipment | 100 | 86.3 | 61.3 | 37.1 | 19.5 | 3.7 | 0.4 | 0.0 | 0.0 |
| 43 | Electric Measuring Instruments | 100 | 99.6 | 93.9 | 73.9 | 40.0 | 1.3 | 0.0 | 0.0 | 0.0 |
| 44 | Generators and Motors | 100 | 99.9 | 98.9 | 95.7 | 89.0 | 62.4 | 28.1 | 6.5 | 0.6 |
| 45 | Relay Switches and Switchboards | 100 | 91.0 | 77.2 | 62.7 | 49.2 | 27.8 | 14.3 | 6.8 | 3.0 |
| 46 | Transformers and Reactors | 100 | 93.2 | 80.3 | 65.4 | 50.8 | 26.9 | 12.3 | 4.9 | 1.7 |
| 47 | Batteries | 100 | 87.2 | 53.1 | 21.3 | 5.4 | 0.1 | 0.0 | 0.0 | 0.0 |
| 48 | Passenger Cars | 100 | 86.6 | 48.8 | 15.9 | 2.8 | 0.0 | 0.0 | 0.0 | 0.0 |
| 49 | Trucks | 100 | 87.3 | 53.7 | 21.9 | 5.7 | 0.1 | 0.0 | 0.0 | 0.0 |
| 50 | Buses | 100 | 96.9 | 86.0 | 68.4 | 48.2 | 15.9 | 2.9 | 0.3 | 0.0 |
| 51 | Ships | 100 | 99.0 | 92.2 | 75.9 | 51.8 | 10.6 | 0.5 | 0.0 | 0.0 |
| 52 | Transport Equipment for Industry Use | 100 | 90.8 | 74.0 | 55.6 | 39.0 | 15.9 | 5.3 | 1.4 | 0.3 |
| 53 | Photographic and Optical Instruments | 100 | 72.7 | 54.5 | 41.2 | 31.4 | 18.5 | 11.0 | 6.6 | 4.0 |
| 54 | Professional and Scientific Instruments | 100 | 89.2 | 64.6 | 38.2 | 18.6 | 2.5 | 0.2 | 0.0 | 0.0 |
| 55 | Analytical Instruments | 100 | 92.5 | 68.3 | 38.0 | 15.4 | 0.9 | 0.0 | 0.0 | 0.0 |
| 56 | Measuring Instruments | 100 | 88.9 | 64.5 | 38.7 | 19.4 | 2.9 | 0.2 | 0.0 | 0.0 |
| 57 | Testing Instruments | 100 | 97.6 | 87.2 | 68.5 | 46.0 | 11.7 | 1.2 | 0.0 | 0.0 |
| 58 | Information Recording Media | 100 | 75.6 | 41.7 | 18.1 | 6.4 | 0.5 | 0.0 | 0.0 | 0.0 |
| 59 | Miscellaneous Products | 100 | 82.0 | 51.6 | 26.3 | 11.0 | 1.2 | 0.1 | 0.0 | 0.0 |
| 60 | Residential Buildings | 100 | 99.5 | 96.8 | 90.6 | 80.4 | 51.3 | 22.9 | 6.5 | 1.1 |
| 61 | Storehouses | 100 | 97.7 | 92.7 | 85.8 | 77.8 | 60.5 | 43.8 | 29.8 | 19.1 |
| 62 | Office Buildings | 100 | 95.7 | 85.6 | 72.4 | 58.1 | 32.3 | 14.9 | 5.8 | 1.9 |
| 63 | Stores | 100 | 93.5 | 81.4 | 67.3 | 53.3 | 29.9 | 14.7 | 6.4 | 2.5 |
| 64 | Factories | 100 | 95.9 | 87.5 | 76.7 | 65.0 | 42.6 | 24.9 | 13.2 | 6.4 |
| 65 | Road and Parking Areas | 100 | 85.5 | 68.4 | 52.9 | 39.8 | 21.3 | 10.7 | 5.1 | 23 |
| 66 | Other Construction | 100 | 95.7 | 78.1 | 50.7 | 24.8 | 2.1 | 0.0 | 0.0 | 0.0 |



Fig. $11 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 1-12

(a) 13.Pumps and Compressors

(d) 16.Machinist's Precision Tools
(g) 19.Food Processing Machinery


(h) 20.Printing and Bookbinding Machinery
(e) 17.Industrial Robots

(k) 23.Other Office Machinery

(c) 15.Metal Processing Machinery

(f) 18.Construction Machinery

(i) 21.Chemical Machinery

(b) 14.Metal Machine Tools


(j) 22.Semiconductor Making Equipment

(l) 24.Machinery for Service Sector

Fig. $12 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 13-24


Fig. $13 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 25-36


Fig. $14 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 37-48


Fig. $15 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 49-60


Fig. $16 S_{0}(\tau)$ and the Weibull Survival Distribution: Assets 61-66

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[^0]:    *This study is implemented in our project for revising capital measurement at ESRI (Economic and Social Research Institute, Cabinet Office). I thank Tadao Futakami (Director of National Wealth Division, ESRI) for his support. The results we report in this paper are preliminary. Comments are welcome.

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[^1]:    ${ }^{4}$ See Nomura and Futakami (2005) for the current problems in official estimates of consumption of fixed capital (CFC) and capital stock in the Japan's national accounts.
    *2 The NWS was implemented twelve times from 1905 to 1970, by the different ministries, government offices, and Bank of Japan. The problems in the current stock measurement in the Japanese national accounts may stem from the fact that its methodology and parameters still depend on the 1970 NWS. The table below reports the history of the Japanese NWSs.

[^2]:    *3 We use the name of productive capital stock after Triplett (1996, 1997) and Hill (1998, 1999). Biorn (1989) and Biorn, Holmoy, and Oystein (1989) call a productive capital stock in this paper a "gross" capital stock, since they do not need a traditional gross concept of capital stock. Blades (2001) does not give a particular name for the productive capital stock.

    Net capital stock in this paper is also called "wealth" capital stock, like Triplett (1997). The net capital stock is "generally, a synonym for the wealth capital stock. The "net" language thus distinguishes the depreciated capital stock (the wealth capital stock) from the undepreciated, or gross capital stock. However, the traditional "gross-net" capital dichotomy does not encompass the productive capital stock, which could cause confusion (because the productive capital stock is "net" of depreciation, compared to the undeteriorated gross stock). Once the distinction between productive and wealth capital stocks fully enters the lexicon, it will probably be preferable to avoid the net capital stock terminology." (Triplett, 1997) However, we use net capital stock in this paper, partly because we cannot find an adequate term in Japanese corresponding to "wealth capital stock," and partly because net capital stock is identical with the traditional net capital stock, although the concept is clarified.

    * Disposal in Blades (2001) is identical with its definition in the 1993 SNA. In the 1993 SNA (United Nations, 1993), "Disposals of assets (inventories, fixed assets or land or other non-produced assets) by institutional units occur when one of those units sells or transfers any of the assets to another institutional unit; when the ownership of an existing fixed asset is transferred from one resident producer to another, the value of the asset sold, bartered, or transferred is recorded as negative gross fixed capital formation by the former and as positive gross fixed capital formation by the latter." (paragraph 10.40).

[^3]:    *5 "The best results are obtained where the retirement observations are made on large numbers of units at regular intervals over several years, and where records of the units in service, as well as those retired from service are available. Because of small numbers of units or infrequent and irregular observations, or both, the resulting curves posses irregularities which are not natural to the general behavior of large properties. These poorly shaped curves must be used, however, but their use is made easier and the results more plausible by an initial smoothing process."(Winfrey, 1935, p.37).

    * Also, for the measurement of infrastructure in Japan, CAO assumes the SE as a discard distribution. See Infrastructure in Japan (in Japanese) in 1986 and 1998.
    *7 In the old OECD Manual on measuring capital, Ward (1976) wrote "The gross stock estimates appear to be more sensitive

[^4]:    to changes in the assumed average lives of assets than to variations in the survival functions. Studies made by OECD have shown that perpetual inventory models based in turn on Winfray S-3, gamma-probability density and rectangular survival distributions [this is identical with the SE ] generate capital stock estimates which rarely differ by more than ten percent in any one year and in most cases the differences were very small. Furthermore no one set of estimates appears to be consistently greater than another."(p.35) This old description still provides an evidence for CAO to assume the SE. A quater of a century later, it is clarely described that the use of the SE is unrealistic in the newly revised OECD manual (Blades, 2001).
    ${ }^{* 8}$ The Weibull distribution function is more generally given as $F(\tau)=1-e^{-\left(\frac{t-\phi}{\lambda}\right)^{\alpha}}$, where $\phi$ is the location parameter ( $\tau>\phi$ ). In this paper, we set $\phi=0$. A generalized Weibull family of distributions for survival studies is proposed in Mudholkar, Srivastava, and Kollia (1996).

[^5]:    *The median and mode of $f(\tau)$ are given by $\lambda(\ln 2)^{a^{-1}}$ and $\lambda\left(1-\alpha^{-1}\right)^{a^{-1}}$, respectively. The figure below displays the comparison

[^6]:    -11 The asset classification coinsts of (1)buildings, (2)construction, (3)machinery and equipment, (4)ships, (5)other transportation equipment, (6)tools and other equipment, (7)miscellaneous products, and (8)construction in progress. Only for the investment survey, the ninth asset: (9)land development is added. The capital groups consist of (1) 30 to 50 million yen, (2) 50-100 million yen, (3) 100 million - 1 billion yen, (4) 1-5 billion yen, (5) over 5 billion yen.
    ${ }^{* 12}$ In the FSSC for the 2002 fiscal year, the number of samples is 29,423 and the effective responses is 23,840 (the response rate is 81.0 percent) for corporations except finance and insurance. Although the number of samples is much larger than that of the 2002-SASD, the FSSC is not sufficient enough to measure capital stock, since it has no asset classification of tangible assets.

[^7]:    ${ }^{-13}$ Gellatly, Tanguay, and Yan (2002) estimates economic depreciation using selling or discard price of asset. Although SASD also investigates value of asset scrapped or sold, it is not clear whether the value is evaluated by the price at the period to be sold or its book value in the 2002-SASD. Improving this questionnaire at the future investigation, we may make it possible to estimate the age-price profile.
    ${ }^{-14}$ As well as the differences in the periods of the purchases, the months of the discards differ among the samples $i$ although they are retired in the same fiscal year. We used the monthly price indexes of the Corporate Goods Price Index (CGPI) produced by

[^8]:    ${ }^{15}$ Fortunately, there may be no length-biased sampling, which is the problem that the data with short duration are underrepresented in the sample. Sce Kiefer (1988) for the case of unemployment duration.

[^9]:    ${ }^{16}$ In the methodology of the Statistics Netherlands (Meinen, Verbiest, and Wolf, 1998) to estimate the retirement patters, a true pdf is approximated by the retirement value over investment, or a hazard function is approximated by the retirement value over gross capital stock. Their estimates do not be affected by the biases we depict here. Statistics Netherlands introduced in 1991 a directly observed survey for discard (Meinen, Verbiest, and Wolf, 1998; Smeets and Hove, 1997). The disinvestments inquiry 1991 was distributed to 1500 large companies in the manufacturing industry (all companies with 100 employees or more) and the response rate was higher than 90 percent (Smeets and Hove, 1997).

[^10]:    *17 Based on more directly observed data for manufacturing, Meinen, Verbiest, and Wolf (1998) reports that it resulted in an average service life for computers of 12 years. They evaluate this estimate as too high and use 5 years as a best-practice estimate for their measurement of gross capital stock.
    ${ }^{41}$ Here, the quantity index of investment is defined approximately as the real investment of non-residential buildings for the private sectors in Nomura (2004).

[^11]:    ${ }^{-19}$ Note that there is less cellular phones in the samples. Thus, 41.wireless communication equipment almost consists of old-type radio communication equipment.

[^12]:    *20 We used the "Wagakuni no Jidousha Hoyuu Doukou", which means current possession status of motor vehicles in Japan, produced by Automobile Inspection and Registration Association (AIRA), supervised by Ministry of Land Infrastructure and Transport, Government of Japan. In this paper, we introduce our estimates only on the possession status in March 2004. We plan to report more detailed results of discard patterns based on some registration data in the end of 2005.

