# **KEO DISCUSSION PAPER**



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Flow of Funds Analysis: The Triangulation and The Dispersion Indices

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### 1. Introduction

Flow of funds (FOF) analysis has been stem from "Social Accounting for Money flows" authored by Morris Copeland in 1949. Since then it has developed as an accounting system describing the inter-sectoral financial transactions between the economic actors. FOF accounts were included in the System of National Accounts in 1968 along with National Income Accounts, National Balance Sheet, Balance of International Payments Accounts and Input-Output Tables. FOF Accounts consist of balance sheets of the economic actors, in their traditional tabulation practice. This format of FOF is widely employed because of the easiness of compilation based on the corporate accounting system. The analysis of FOF based on the balance sheet format has been concentrated on the investigation of the difference between financial assets and liabilities of each sector. However this kind of study only describes the final balance of object economy and the portfolio selection activity of the economic actors. It is unavoidable to build an asset-liability-matrix (ALM) to examine the inter-sectoral financial transactions on the whole. The first purpose of this paper is to present the compilation procedure of ALM from the FOF accounts of the balance sheet format widely available. The second purpose of this article is to show the interdependency among economic actors participating in the financial market, in terms of the triangulation and the dispersion indices. In this paper, FOF tables for Japan (March, 2000) will be employed for the demonstration.

As Leontief mentioned<sup>1</sup>, dependence and independence, hierarchy and circularity are the four basic concepts of structural analysis. The definition and practical significance of each of these ideas can be demonstrated visually by schematic model tables in which numbers signify the presence or absence of interindustry transactions. As in case of input-output tables, if the corresponding box formed by the reverse combination of column and row is empty. Such relations become clearer in the model in which all the positive numbers fall below the diagonal running from the upper left corner to the lower right corner of the matrix. Rearrangement of the rows and columns of the original ALM as well as the input-output matrix construct this "triangular" system.

In addition to triangulation, the introduction of ALM into the framework of FOF analysis enables us to utilize the affluent assets of Input-Output (I-O) analysis notably the concept of Leontief-Inverse. However there are not a few fundamental differences between the ALM analysis and the I-O analysis. In the Y-table of the ALM, which is the sector-by-sector matrix, the column denotes the portfolio of fund-raising, while the row

<sup>&</sup>lt;sup>1</sup> Leontief(1966), pp.166-168.

indicates the portfolio of fund-employment of a particular sector. In this sense, the ALM is an I-O matrix that is descriptive of the flow of funds. However it is also possible to construct an ALM that gives an account of the flow of financial instruments instead of the flow of funds. The column of this type of ALM (Y\*-table) denotes the portfolio of fund-employment, while the row indicates the portfolio of fund-raising. In this context, the Y\* matrix is a transposition of Y matrix.

This two-sided nature of ALM gives a significant theoretical importance to the FOF analysis. The simultaneous equations symbolised by Y portray the relations between the surplus in liabilities and the controlled total, while those represented by Y\* depict the correspondence between the surplus in financial assets and the controlled total. The coexistence of these two systems of equations gives two alternative Leontief-Inverses to the structure of ALM. In the last part of this exposition, we will examine the asymmetric nature of the system in terms of the column sum and the row sum of the Leontief-Inverse, namely the indices of the power and the sensitivity of dispersion.

### 2. The Asset Liability Matrix

### 2.1 E- and R-tables

In Japan, Flow of Funds Accounts are compiled on the basis of 1993 IMF Manual by BOJ every three month. The ALM used in this paper has been compiled from the Financial Assets and Liabilities tables of FOF of 1st quarter 2000. The first step to draw up ALM is to pick out the assets and liabilities vectors separately from the balance sheets of FOF to make out two matrices E and R. E is a matrix to show the portfolio of fund employment of each sector,  $\varepsilon$  and T<sup>E</sup> are vectors that represent excess liabilities, sum of each row. Likewise, R is a matrix to show the portfolio of fund raising of each sector,  $\rho$  and T<sup>R</sup> are vectors that represent excess assets, sum of each row respectively. T is the vector that consist of either the sum of assets or liabilities whichever are greater. n and m denote the number of financial instruments and the number of institutional sectors. The structure of E and R tables in terms of their components are depicted below.

<i>e</i> <sub>11</sub>	$e_{12}$	•••	$e_{1m}$	$t_1^E$	$r_{11}$	<i>r</i> <sub>12</sub>	•••	$r_{1m}$	$t_1^R$
$e_{21}^{}$	e 22	•••	$e_{2m}$	$t_2^E$	$r_{21}$	<i>r</i> <sub>22</sub>	•••	r <sub>2m</sub>	$t_2^R$
:	:	۰.	÷	:	:	÷	·.	÷	:
e <sub>nl</sub>	<i>e</i> <sub>n2</sub>	•••	e <sub>nm</sub>	$t_n^E$	$r_{nl}$	$r_{n2}$	•••	r <sub>nm</sub>	$t_n^R$
$\varepsilon_1$	$\varepsilon_{_2}$	•••	$\mathcal{E}_m$		$ ho_1$	$ ho_2$	•••	$ ho_{m}$	
$t_1$	$t_2$	•••	t <sub>m</sub>		$t_1$	$t_2$	•••	t <sub>m</sub>	
	Figu	re 1:	E·tab	le	Fi	gure	2: R	table	

### 2.2 Y- and Y\*-tables

The ALM based on the fund-raising portfolio is denoted as Y while the one based on fund-employment is symbolized as Y<sup>\*</sup>. We use Superscript letter <sup>\*</sup> in case fund-employment assumption is concerned. To compile Y table in accordance with fund-raising portfolio, first R matrix is substituted for U matrix (commodity by sector) and transposed E matrix for V matrix (sector by commodity).

$$\mathbf{U} \equiv \mathbf{R}$$

$$\mathbf{V} \equiv \mathbf{E'}$$

In case of Y\* table that represent fund employment portfolio, we take E matrix as  $U^*$  matrix and transposed R matrix as V\* matrix.

 $\mathbf{U}^* \equiv \mathbf{E}$ 

 $V' \equiv R'$ 

The coefficient matrices, B and B<sup>\*</sup>, are constructed from U, U<sup>\*</sup> and T by dividing the cells in each column of U and U<sup>\*</sup> by the column sums T.

$$b_{ij} = \frac{u_{ij}}{t_j}$$

$$b_{ij}^* = \frac{u_{ij}^*}{t_j}$$

In the same manner, coefficient matrices D and D\* corresponding to V and V\*are defined as follows:

$$d_{ij} = \frac{v_{ij}}{t_j^E}$$

$$d_{ij}^* = \frac{v_{ij}^*}{t_j^R}$$

where  $t^{E_j}$  is the sum of assets and  $t^{R_j}$  is the sum of liabilities for financial instrument j. That is,  $d_{ij}$  is regarded as i sector's share of assets for j financial instruments while  $d^{*_{ij}}$  is i sector's share of liabilities for j financial instruments. The m x m coefficient matrices C and C\* corresponding to Y and Y\* are estimated using actor portfolio assumption, which is an equivalent of the industry technology assumption in the scheme of I-O analysis.

## $\mathbf{C} = \mathbf{D}\mathbf{B}$

## $\mathbf{C}^{\star} = \mathbf{D}^{\star}\mathbf{B}^{\star}$

Using these matrices, C and C\*, transaction quantity matrices Y and Y\* are reduced in

the following manner:

$$y_{ij} = c_{ij}t_j$$

$$y_{ij}^* = c_{ij}^* t_j$$

where  $y_{ij}$  is the amount of funds provided from sector i to sector j, and  $y^*_{ij}$  is the amount of financial instruments supplied from sector i to sector j. These tables are shown in Fig. 3 and Fig.4.

When we compare Y<sup>\*</sup> table with Y table,  $\varepsilon^{Y}$  vector and  $\rho^{Y}$  vector are situated symmetrically. Moreover matrix Y<sup>\*</sup> is obtained by interchanging matrix Y's rows and columns, i.e. matrix Y<sup>\*</sup> is a transpose matrix of Y. As demonstrated in the Appendix, whether we adapt fund raising assumption or fund employment assumption, only one transaction quantity matrix is derived from a pair of matching E<sup>\*</sup> and R<sup>\*</sup>matrices. In that sense, the matrices Y and Y<sup>\*</sup> are just like two sides of the same coin.

<i>Y</i> 11	$y_{12}$	•••	$\mathcal{Y}_{1m}$	$\varepsilon_1^r$	$t_1^{Y}$	y <sup>*</sup> 11	$y^{*}_{12}$	•••	$y_{1m}^*$	$\rho_1^r$	$t_1^{\gamma}$
$y_{21}$	${\cal Y}_{22}$	•••	$y_{2m}$	$\varepsilon_2^{r}$	$t_2^{Y}$	<i>y</i> <sup>*</sup> <sub>21</sub>	y*22	•••	y*2m	$ ho_2^{ m r}$	$t_2^{Y}$
			:				:	·.	:	:	:
$\mathcal{Y}_{m1}$	$y_{m2}$	•••	y <sub>mm</sub>	$\varepsilon_m^{Y}$	$t_m^{Y}$	<i>y</i> * <i>m</i> 1	y* <sub>m2</sub>	•••	<i>y</i> * <sub>mm</sub>	$\rho_m^{Y}$	$t_m^{Y}$
$\rho_1^{r}$	$\rho_2^{ m r}$	•••	$\rho_m^{Y}$			$\varepsilon_1^r$	$\varepsilon_2^{r}$	•••	$\varepsilon_m^{Y}$		
$t_1^r$	$t_2^{r}$	•••	$t_m^{Y}$			$t_1^{\gamma}$	$t_2^{r}$	•••	$t_m^{Y}$		
Fi	gure	3: Y-t	able				Figur	e 4: Y	/*-table		

So far, it is expressed that two kinds of ALM are drawn up in compliance with the difference of behavioural pattern whether raising funds or employing them. One is Y-table which is based on the assumption that each sector have fixed fund-raising portfolio (Liability Approach), the other is Y\*-table which is founded on the assumption that fund-employment portfolio of each sector is settled (Asset Approach). Fig. 5 and 6 show tables of funds transactions and coefficients of which Liability Approach consist. Asset Approach is composed of tables given in the same way in Fig. 7 and 8; a superscript figure \* is put in distinction from Liability Approach. Following analysis in this paper is made using Y-table in March 2000, which is presented in Table 1.

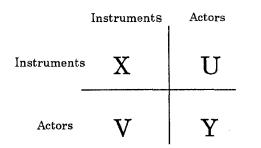


Figure 5: Tables of funds transactions based on Liability Approach

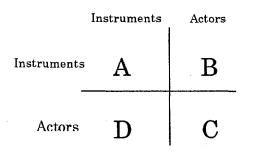
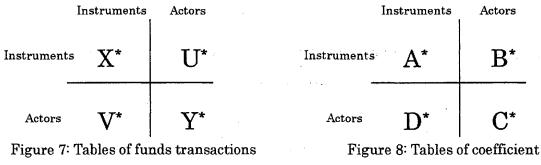


Figure 6: Tables of coefficient based on Liability Approach



based on Asset Approach

# based on Asset Approach

### 3 The triangulation of ALM

Since sectors and activities included in I-O or FOF are randomly ordered in usual cases, one glance is not enough to grasp the mutual relation within the system. So that we rearrange the rows and columns of the original ALM to analyse a causal sequence and ranking within the financial economy.

In case of triangulation of ALM, first we net out the symmetrical elements in Y matrix and then omit transaction figures less than 10 billion yen. Then sorting actors of Y matrix to minimum the number of upper right elements of Y matrix, it would prove that there are one way flow of funds and clear relation of cause and effect in ALM. Table 2 presents the result of triangulation of ALM in March 2000. 84 elements out of all 595 elements that are upper right of Y matrix are null. It accounts for 13.3 percent of the total number of upper right elements. The order of the actors set on the basis of minimizing the number of upper right elements is showed in Table 3. Actors that depend on many other actors for supply of funds are situated in the upper side of table. These actors themselves tend to employ funds in a limited number of other actors, and themselves serve many actors with funds are in the lower side of the table. Public

non-financial corporations are in the first place and private non-financial corporate enterprises are in the second place, then central government and rest of the world follow them. These actors have common characteristics that they make an excess investment over saving. On the contrary, actors situated in the bottom are public pension funds, households, corporate pensions, mutual aid insurance and so on. Households have excess savings and then public pensions etc. receive funds directly from them. We could compare Japanese financial system to a current in the river that rise from households, go through financial institutions of various kinds, and then flow into non-financial corporations and government downstream. It should be noted that not only financial institutions but also local governments and private non-profit institutions serving households are situated in the middle place.

	Actors
1	Public non-financial institutions
2	Private non-financial corporate enterprises
3	Central government
4	Rest of the world
5	Money market dealers
6	Special accounts for foreign reserve funds
7	Foreign-owned banks in Japan
8	Finance companies
9	Postal savings
10	Local governments
11	Securities companies
12	Deposit insurance organization etc
13	Licensed commercial and investment banks
14	Private non-profit institutions serving households
15	Government financial institutions
16	Bank of Japan
17	Collectively managed trusts

Tabl	e 3:	Α	resul	t ta	able	of	triang	ulation
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e of tri	angulation
18	Non-collectively managed trusts
19	Stock investment trusts
20	Other bond investment
21	Structured financing special purpose
	companies and trusts
22	Financial institutions for small business
23	MMF/MRF
24	Financial institutions for agriculture, forestry
	and fisheries
25	Other non-life insurance institutions
26	Private non-life insurance companies
27	Trust fund bureau
28	Private life insurance companies
29	Other social security funds
30	Postal life insurance
31	National pension funds etc.
32	Mutual aid insurance
33	Corporate pensions
34	Households
35	Public pension funds

### 4 Leontief Inverse of Y. and Y\*-tables

#### 4.1 methodologies

We will apply the Leontief-Inverse, namely the indices of the power and the sensitivity of dispersion to Flow of Funds analysis. First denoting two vectors  $\varepsilon^{\gamma}$  and  $\rho^{\gamma}$  as follows:

$$\boldsymbol{\varepsilon}^{\mathbf{Y}} = \begin{bmatrix} \boldsymbol{\varepsilon}_{1}^{\mathbf{Y}} \\ \boldsymbol{\varepsilon}_{2}^{\mathbf{Y}} \\ \vdots \\ \boldsymbol{\varepsilon}_{m}^{\mathbf{Y}} \end{bmatrix} \quad \boldsymbol{\rho}^{\mathbf{Y}} = \begin{bmatrix} \boldsymbol{\rho}_{1}^{\mathbf{Y}} \\ \boldsymbol{\rho}_{2}^{\mathbf{Y}} \\ \vdots \\ \boldsymbol{\rho}_{m}^{\mathbf{Y}} \end{bmatrix}$$

The fundamental equations respect to Y and Y\*-tables are expressed as follows:  $\mathbf{C} \cdot \mathbf{T}^Y + \boldsymbol{\epsilon}^Y = \mathbf{T}^Y$ 

$$\mathbf{C}^{\star} \cdot \mathbf{T}^{\mathbf{Y}} + \mathbf{\rho}^{\mathbf{Y}} = \mathbf{T}^{\mathbf{Y}}$$

Solving each equation for T<sup>Y</sup> yields

$$\mathbf{T}^{\mathbf{Y}} = (\mathbf{I} - \mathbf{C})^{-1} \boldsymbol{\varepsilon}^{\mathbf{Y}}$$
$$\mathbf{T}^{\mathbf{Y}} = (\mathbf{I} - \mathbf{C}^{\star})^{-1} \boldsymbol{\rho}^{\mathbf{Y}}$$

where I denotes the m x m unit matrix,  $(I-C)^{-1}$  is the m x m Leontief inverse matrix by which how much demand for funds would be induced to each sector can be calculated, and  $(I-C^*)^{-1}$  is the m x m Leontief inverse matrix by which we can calculate the amount of ultimately induced supply of funds. These matrixes are denoted  $\Gamma$  and  $\Gamma^*$  as follows,

$$\boldsymbol{\Gamma} = (\mathbf{I} - \mathbf{C})^{-1} = \begin{bmatrix} \gamma_{11} & \gamma_{12} & \cdots & \gamma_{1m} \\ \gamma_{21} & \gamma_{22} & \cdots & \gamma_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ \gamma_{m1} & \gamma_{m2} & \cdots & \gamma_{mm} \end{bmatrix}$$
$$\boldsymbol{\Gamma}^{*} = (\mathbf{I} - \mathbf{C}^{*})^{-1} = \begin{bmatrix} \gamma^{*}_{11} & \gamma^{*}_{12} & \cdots & \gamma^{*}_{1m} \\ \gamma^{*}_{21} & \gamma^{*}_{22} & \cdots & \gamma^{*}_{2m} \\ \vdots & \vdots & \ddots & \vdots \\ \gamma^{*}_{m1} & \gamma^{*}_{m2} & \cdots & \gamma^{*}_{mm} \end{bmatrix}$$

where  $\gamma_{ij}$  describes the amount of increase in demand for i sector's funds when the demand for j sector's funds rise, and  $\gamma^*_{ij}$  is the amount of increase in funds for which i sector derives supply, when j sector is supplied with funds. We can calculate both indices

of the power of dispersion and of the sensitivity of dispersion using  $\gamma_{ij}$  or  $\gamma^*_{ij}$ . Since the meaning of  $\gamma_{ij}$  is different from that of  $\gamma^*_{ij}$ , four distinct index would be made as follows.

$$w^{r}{}_{j} = \frac{\sum_{i=1}^{m} r_{ij}}{\frac{1}{m} \sum_{j=1}^{m} \sum_{i=1}^{m} r_{ij}}$$
$$w^{r}{}_{j} = \frac{\sum_{i=1}^{m} r^{*}{}_{ij}}{\frac{1}{m} \sum_{j=1}^{m} \sum_{i=1}^{m} r^{*}{}_{ij}}$$
$$z^{r}{}_{i} = \frac{\sum_{j=1}^{m} r_{ij}}{\frac{1}{m} \sum_{i=1}^{m} \sum_{j=1}^{m} r_{ij}}$$
$$z^{r}{}_{i} = \frac{\sum_{j=1}^{m} r^{*}{}_{ij}}{\frac{1}{m} \sum_{i=1}^{m} \sum_{j=1}^{m} r^{*}{}_{ij}}$$

where  $w^{Y_j}$  and  $w^{Y*_j}$  given by  $\gamma_{ij}$  and  $\gamma^{*_{ij}}$  respectively are indices of the power of dispersion and  $z^{Y_i}$  and  $z^{Y*_i}$  are indices of the sensitivity of dispersion. We name  $w^{Y_j}$  as the dispersion power index of fund-raising,  $w^{Y*_j}$  as the dispersion power index of fund-employment,  $z^{Y_i}$  as the dispersion sensitivity index of fund-raising, and  $z^{Y*_I}$  as the dispersion sensitivity index of fund-employment.

### 4.2 Results

The relation of the dispersion power index of fund-raising,  $w^{Y}_{j}$ , and the dispersion power index of fund-employment,  $w^{Y*}_{j}$ , is presented in Fig.9. Households, the primary saving subject (fund-employer), and public pensions and other social security funds that specialize employing funds provided from households are situated in the second quadrant. Non-financial corporations, the primary investing subject (fund-raiser), and central government that is deeply in financial debt are in the fourth quadrant. Judging from the difference of fund-raising from fund-employment, these results are just as expected. Licensed commercial and investment banks, structured-financing special purpose companies and government financial institutions, which intermediate between primary saving subject and primary investing subject are in the first quadrant. The biggest intermediating institution of funds, licensed commercial and investment banks, whose values of both indices about 1.1, lie between the biggest saving subject, households, and major investigating subject, private non-financial corporate enterprises. The central bank, Bank of Japan is found in the fourth quadrant compared with money market dealers sited in the first quadrant. It shows that the latter have more effect on financial market than the former.

The relation of the dispersion sensitivity index of fund-raising,  $z^{Y_i}$  with the dispersion sensitivity index of fund employment  $z^{Y_{i}}$  is presented in Fig.10. Though the dispersion sensitivity index is expected as the transposition of dispersion power index, there are households as well as private non-financial corporate enterprises in the first quadrant and they lay facing each other with a line of 45 degrees between. This means that both subjects play important parts in the financial system. Households save but also invest in housing as well, and private non-financial corporate enterprises not only raise funds but also play as moneylender. On the contrary big investment subjects, central government and rest of the world, are not major in supply of funds in view of their little value of the dispersion sensitivity index of fund-raising. Most of all financial institutions belong to the third quadrant while public financial institutions including licensed commercial and investment banks, postal savings, trust fund bureau and government financial institutions are in the first; and financial institutions for agriculture, forestry, and fishers, financial institutions for small business and public pensions are in the fourth. It may be caused by that most of financial institutions deal with many and unspecified partners.

### **5** Conclusions

In a framework of FOF table, the only object to be traded in it is fund, an abstract object. Moreover, there is a reversed flow of financial instruments, either material or fictitious, wherever there is flow of funds. By focusing on these two things, we have compiled two kinds of ALM, one based on fund-raising-portfolio assumption (Liability Approach) and another based on fund-employment-portfolio assumption (Asset Approach). It has been confirmed that these two different approach produce no less than a pair of twin transposed matrices. This means that no matter which method we might employ, one consistent ALM is derived from a set of E and R tables transformed from balance-sheet-type FOF tables universally available in most of OECD and IMF member countries.

Not a few techniques have been proposed to examine the fundamental character of an I-O table. We have chosen two of them namely the triangulation and the dispersion indices to apply on FOF analysis. By rearranging rows and columns of the original ALM,

we could successfully form a quasi-triangle matrix. This means that those actors that raise funds from multifarious sources tend to employ them in limited number of ends while those actors that raise funds from limited sources tend to employ them in various objects. An instant survey of the financial system gives a picture in which the funds proceeds from the household, the primary saving subjects, goes through the intermediaries, like commercial banks and other financial institutions, and ends up in the non-financial corporate enterprises, the primary investing subjects. The primary investors, including non-financial corporate enterprises and the central government, raise funds from many sectors by issuing bonds and/or stocks and allot them directly to production facilities or public works. On the other hand, the households, the primary saving subjects, and the institutional investors including pension funds and life insurers, which collect funds directly from the households, allocate the assets to a variety of objects in view of risk diversification. In the middle stream of the flow of funds, intermediary financial institutions, including commercial banks as well as the central bank, are situated alongside of the local governments and nonprofit institutions like educational foundations and religious corporations. These middle-stream institutions collect funds not only from the household but also from some of their fellow intermediaries and employ them directly or indirectly in the final investments.

In the course of the dispersion indices analysis, we found that there is an asymmetry in the propagation process of fund-raising and fund-employment. For example, in case of households, the primary saving subjects, the dispersion power index of fund-raising is less than one while that of fund-employment is greater than one. On the contrary, in case of non-financial corporate enterprise, the primary investing subject, the dispersion power index of fund raising is greater than unity while that of fund employment is less than unity. In this sense, the primary saving subjects and the primary investing subjects are both extremes in a financial system. However, as for the dispersion sensitivity indices of fund-raising and fund-employment, those of both households and non-financial corporate enterprises are greater than one. This might be because the household, the primary saver, make housing investments in residential buildings, and the non-financial corporate enterprise, the primary investor, sell their products to customers on credit and make advance payments to their subcontractors. As a conclusion, it can be said that the dispersion power index reflects the primary nature of the actors while the dispersion sensitivity index exhibits the exact nature of them. By introducing four different definitions of dispersion indices, it is possible to reconstruct them in a multidimensional space, so that we can clarify the role and the position of the economic actors in the financial system more explicitly.

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6	1929	116463	56313	0	3005	37100	1642	454751		13	55	44	2338	23586	43451	ō	1064742
	30406	102688	52245	15908	128650		-	577524		174173	503	655	1270690	65597	409471	172741	7489182
	2891	25308	8157	28	5869			59600		5209	53	R	24022	5745	29906	0	403114
	8572	16404	13676	8566	14791	299512	25294	74690	2612	25897	21	27	121036	9144	120862	0	1762134
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2588680	13903	8646	645	3311	888			285942		89659	579	220	2411	535	76260	0	3210413
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0	15848	41734	12571	12616	12214			261715	21221	61839	135	177	124349	7333	146270	0	1563681
29488	181065	8624	872	4740	2417			292303		103887	11014	36	9497	2864	69183	a	1176293
٥	3249	5246	3385	3042	1682			12967	176	13590	172	223	13173	714	41294	Ó	342758
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0	14336	942	1892	3867				97233		42710	e	4	4237	521	22388	0	362726
0	4340	10317	4114	5294				122846	3069	19161	24	32	10892	6961	165790	0	825786
8155	4356	2069		1391				25697		3122	ŝ	2	1203	205	14003	0	132904
0	1041	693		1853		25443		36532	0	4631	0	•	0	58	26486	0	208243
٥	1374	166		753	31	17151		50107	•	6002	•	•	2	59	34592	695	179073
a	64	3922		290		93984		6681	0	20	0	•	56	37	29758	301	169963
٥	5090	7220	176	326		461577		15052	0	10611	278	360	312878	8185	39484	237030	1342378
٥	628	1245		651		74288		110	0	561	16	4	26260	437	3342	0	120501
a	1117448	25110	3110	0	2270	349485		1114939	0	423122	140248	0	106954	34073	140957	ö	4498408
3443	318561	7637	354	1691	681	201809		131568	0	125392	41459	<b>6</b> 8	9801388	9713	54446	5	2035217
o	6699	194109	0		1139	596191	10255	83039	4325	981	105	128	23620	20859	53552	65950	930220
0	ç	37820	68641	80	0	394		3214	208	•	<b>0</b>	•	15	8372	557	0	328759
¢	3773	6963		21312	538	140190	6603	63345	10258	3671	0	0	1926	350	63640	0	438174
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0	31759	8282	118	1762	1795	-	83629	30337		1159	66	144	8008	1579	20560	507404	1248621
1490230	30701	38279	2071	6287	1034	-	53697	110297	66	26293	272	413	11163	7544	80075	ō	2215605
84969	3465	4924	63	33	277		9649	12942	0	1627	42	49	864	338	1533	0	183710
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a	5634	6580	2093	•	120	55687	10622	118414	0	15214	44	501	4559	5173	11 799	0	554522
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