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## INTERNATIONAL DIFFERENCES IN PRODUCTION FUNCTIONS AND FACTOR PRICE EQUALIZATION

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*Abstract:* This is a note on the implication of relaxing the assumption of international trade theory that production functions are identical across countries. A Euclidean measure of the international difference between exponential production functions is used to examine properties of the mapping to implied international differences in factor prices across freely trading countries. For anticipated differences in estimated production functions, factor prices would be similar across countries if factor price equalization would otherwise hold.

### 1. INTRODUCTION

The factor price equalization (FPE) theorem in international trade theory has a curious history. It was discovered without fanfare in the 1930s by Lerner (1952), then independently formalized by Samuelson (1949). Chipman (1966) presents a history of its logic and historical development. While FPE has stirred some controversy over the years, it remains useful as pedagogy and point of reference.

The proof of FPE depends on a number of assumptions:

- (a) free trade and free transport between countries
- (b) cost minimizing firms in a competitive economy
- (c) an identical number of productive factors and international markets
- (d) international factor endowments inside the production cone
- (e) identical neoclassical nonjoint production functions.

If any one of these assumptions is relaxed, FPE loses its logical necessity. Strands in the international trade literature examine the implications of relaxing various assumptions. This paper concentrates on relaxing the assumption of identical production functions.

Consider each assumption in turn. While trade is never entirely free, for many

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traded goods protection and transport costs are small percentages of price. The move toward global free trade is making this assumption more appropriate for many goods.

Cost minimization provides the basis for the theory of the firm, and competitive pricing is a reasonable assumption for the long run in many industries. Factor markets, for the most part, are competitive.

To the extent that factors or goods can be aggregated, their exact numbers should not grossly affect the quantitative nature of the comparative static results of general equilibrium models. Theoretical properties of models with many factors and many goods are developed by Chang (1979), Ethier (1979), Thompson (1987), and others.

With only commonly produced goods entering the argument, factor endowments across many trading countries would likely lie within common production cones, at least for a large portion of observed international trade.

The assumption of identical nonjoint production functions across countries stands out for those with any experience in applied production analysis. Implications of joint production are explored by Samuelson (1992) and Jones (1992). The step from general neoclassical “blackboard” production functions to functional forms which could be estimated and applied is a large one. Identical production functions would first imply that specified production functions for a particular good would have the same functional form (Cobb-Douglas, CES, translog, and so on). Further, estimated technical coefficients would in practice have to be identical across countries.

Estimates of production or cost functions vary for the same industry over time and for different industries in the same sector. On the other hand, similarity of production functions is one criterion for aggregating goods. It is worthwhile to investigate the theoretical implications of allowing some difference in production functions across countries.

The idea that production functions may differ across countries is hardly new to trade theory. The classical Ricardian constant cost model is implicitly built on the assumption of different, if simple, production functions. The technology transfer literature concentrates on technology shift parameters in production functions and the dynamic international transmission of production techniques. Amano (1964) distinguishes between comparative cost differences based on endowment differences and technology shift parameters. Bardhan (1965) uses technology shift parameters in the production functions of the Heckscher–Ohlin model to illustrate that a country with better (Hicks neutral) technology in an industry will have a higher price of the factor used intensively in that industry. Ruffin (1988) develops a Ricardian factor endowment trade model with different production functions across countries in the form of fixed unit input proportions for the different factors of production.

The present study begins to address the impact on factor proportions trade theory of international differences in production functions in the form of different

exponential production coefficients. A measure of the distance between exponential production functions is specified. The focus is on how this measure relates to the implied differences between factor prices across each country's static general equilibrium.

If FPE would otherwise hold, international differences between factor prices go to zero as the distance between production functions goes to zero. More similar production functions between trading partners would generally lead to more similar sets of factor prices. The important underlying empirical issue is the extent to which observed international differences in factor prices are explained by observed differences in production functions.

Empirical tests of the FPE theorem and the Heckscher-Ohlin theorem, starting with Leontief (1953), extending through Leamer (1984), Dollar, Wolff, and Baumol (1988) and Brecher and Choudhri (1993), and surveyed by Deardorff (1984), assume identical production functions everywhere. Direct evidence of international differences in production functions is found, however, by Arrow, Chenery, Minhas, and Solow (1961) and Minhas (1962). Maskus (1990) argues that observed differences in cost minimizing input mixes and the direction of trade together effectively imply different production functions across countries. In spite of the famous classic argument of Pearce (1970) that the laws of physics are the same everywhere, trade theory should in practice be able to proceed under the working assumption that estimated production functions at any point in time would be different across countries.

The foundation of FPE has not been implemented in the fundamental sense of a systematic international comparison of production functions. Intuition from applied production analysis suggests that production functions would not be identical across countries. Indeed, the entire issue can be developed across countries in terms of efficiency frontier analysis. The present paper aims to widen the scope of factor proportions trade theory by explicitly allowing different international production functions.

## 2. THE MAPPING BETWEEN DIFFERENCES IN PRODUCTION FUNCTIONS AND FACTOR PRICES

Consider the set  $F$  of exponential production functions from the vector  $v$  of inputs to a particular output level  $x_0$ :

$$F = \{f: f(v) = \{\prod v_i^{\alpha_i} = x_0\} . \quad (1)$$

A particular production function in  $F$  is characterized by its positive exponents  $\alpha_i$ . For simplicity, concentrate on the set of unit isoquants where  $x_0 = 1$ . The unit level of output  $x_0$  can be produced by any of the production functions in  $F$ . Various combinations of inputs would lead to  $x_0 = 1$  along any particular unit isoquant in  $F$ .

With exponential production functions, the unit isoquants all intersect at the

unit vector. For a given nonunit vector  $v$  of inputs, the various production functions in  $F$  would lead to different levels of output. For any particular production function  $f(v)$ , various input vectors would lead to the same output along an isoquant.

The distance  $d(f, f^*)$  between any two production functions  $f$  and  $f^*$  in  $F$  is a real number defined by some functional. Following Rudin (1976),  $d(f, f^*)$  would qualify as a functional metric if

- (i)  $d(f, f^*) > 0$  when  $f \neq f^*$ , and  $d(f, f^*) = 0$  when  $f = f^*$
- (ii)  $d(f, f^*) = d(f^*, f)$
- (iii)  $d(f, f^*) \leq d(f, f') + d(f', f^*)$  for any  $f'$  in  $F$ .

An example of a metric on function spaces would be

$$d(f, f^*) \equiv \max |f(v) - f^*(v)|, \quad (3)$$

where the vector  $v$  is limited to a closed set. The functional in (3), however, is not differentiable and not useful for the study at hand.

An intuitive metric involves integrating across differences in values of the function. Let  $v$  be a scalar as with Ricardian labor inputs, and consider the metric

$$d(f, f^*) \equiv \int_{\alpha}^{\beta} |f(v) - f^*(v)| dv, \quad (4)$$

where  $\alpha$  and  $\beta$  are limiting elements of  $v$ . The neoclassical Inada conditions imply that  $\alpha > 0$  and  $\beta$  is finite. The choice of the limits of integration in an applied situation would depend on characteristics of the data.

When  $v$  is a vector of inputs, the metric in (4) can be expressed

$$d(f, f^*) \equiv \sum_i \int_{\alpha_i}^{\beta_i} |f(v) - f^*(v)| dv_i. \quad (5)$$

The metric in (5) has geometric and intuitive appeal. The distance between two production functions is essentially defined as the space between the unit isoquants, up to the limits of integration.

Setting these limits of integration is necessary with exponential production functions given that some of every factor is required in production. Isoquants are asymptotic to each axis and the distance between unit isoquants accumulates as they approach an axis. Limits of integration cut off the measure at a relevant range of inputs.

When there are two inputs, the unit isoquant can simply be taken as a function from one input to the other  $v_1 = h(v_2)$  where  $v_i$  represents the input of factor  $i$ . The distance measure in (5) can then be expressed as the simple integral

$$d(f, f^*) = \int_{\alpha_2}^{\beta_2} |h - h^*| dv_2. \quad (6)$$

The international difference in a factor price is measured

$$dw_i = |w_i - w_i^*| \tag{7}$$

where \* represents the foreign variable. For simplicity, consider only cases with  $w_i > w_i^*$ .

Let  $f$  represent the production function for a particular good at home, and  $f^*$  the production function for the same good in the foreign country. If  $d(f, f^*) = 0$  and FPE would otherwise hold,  $dw_i = 0$  for every factor  $i$ . When  $d(f, f^*) = 0$ , the mapping from the vector  $p$  of international prices to the vector  $w$  of factor prices is locally one to one and invertible, at least under other sufficient conditions laid out by Chipman (1966). This is the FPE result. Furthermore, for any given  $d(f, f^*)$  the mapping from  $p$  to  $w$  would also be one to one and invertible.

The relation  $\phi_i$  between  $df \equiv d(f, f^*)$  and the international difference in a particular factor price  $w_i$  is the focus of this study:

$$\phi_i(df) = dw_i. \tag{8}$$

When FPE holds,  $\phi_i(0) = 0$ .

### 3. CHARACTERISTICS OF THE DISTANCE MAPPING

In the Lerner–Pearce diagram of Fig. 1, dotted lines represent a range of differences between exponential production functions for good 1:  $df_1 \equiv d(f_1, f_1^*)$ . Let  $c_j$  represent the cost of a unit of good  $j$ ,  $c_j = w_1 a_{1j} + w_2 a_{2j}$ , where  $a_{ij}$  is the cost

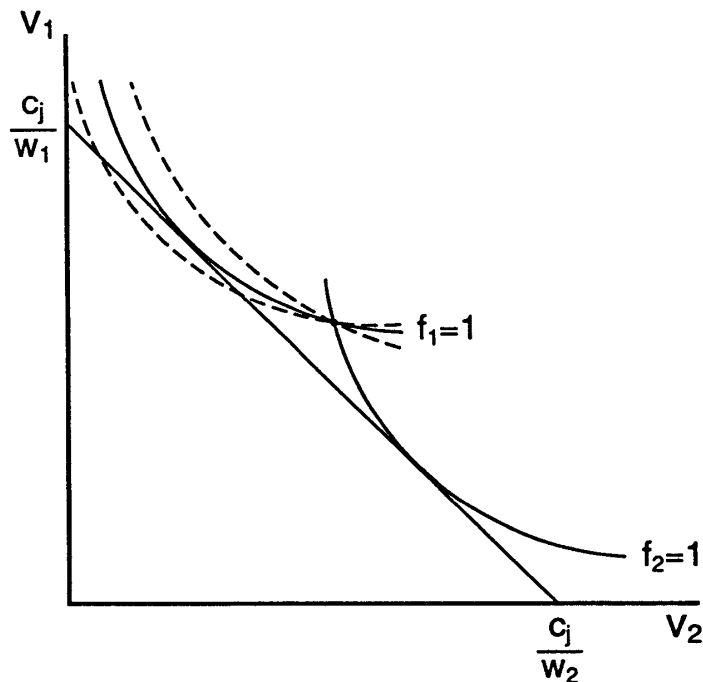


Fig. 1.

minimizing amount of factor  $i$  per unit of good  $j$ . Consider unit value isoquants, where  $p_j = c_j = 1$ . The unit isocost line would then intersect either factor's axis at  $1/w_i$ . If price (and cost) are held constant as a production function varies across countries, the distance between intersections of the isocost line along each axis would reflect the international difference in a factor price.

Assume the position of unit isoquant  $f_2$  in Fig. 1 is the same across countries. Increasing differences in unit isoquant  $f_1$  would create increasing differences in the same factor price across countries with the isocost line adjusting to the cost minimization.

Consider the mapping  $\phi_i$  in (8). With  $w_i > w_i^*$  by construction,  $dw_i = w_i - w_i^*$ . Any particular  $df$  will lead to unique  $dw_i$ , which implies that the two  $\phi_i$  mappings are one to one. Further,  $\phi_i$  is continuous at zero, since

$$\lim_{df \rightarrow 0} \phi_i(df) = \phi_i(0) = 0, \quad (9)$$

a restatement of the FPE result. Continuity of  $\phi_i$  would also follow if for any nonnegative  $N$

$$\lim_{df \rightarrow N} \phi_i(df) = \phi_i(N). \quad (10)$$

Given smooth convex isoquants in both sectors, the  $\phi_i$  mapping would apparently be continuous. Without specifying particular production functions, however, a formal proof that  $\phi_i$  is continuous may be unattainable.

Consider two  $dw_i$  which are arbitrarily close together:  $|dw_i' - dw_i''| < \varepsilon$ , for any  $\varepsilon > 0$ . In other words,  $dw_i'$  lies in the open interval  $W \equiv (dw_i' - \varepsilon, dw_i' + \varepsilon)$ . Let  $dw_i'$  correspond to  $df'$  and  $dw_i''$  to  $df''$ . There should be  $\delta > 0$  such that the set  $D$  defined as  $(df'' - \delta, df'' + \delta)$  is a subset of  $\phi_i^{-1}(W)$ . If  $df'$  were in the open set  $D$ , it would follow that  $\phi_i(df')$  would be in  $W$ , or  $|\phi_i(df'') - \phi_i(df')| < \varepsilon$ . Since  $\varepsilon$  is arbitrarily small,  $\phi_i$  would be continuous at the arbitrary point  $df''$ , and thus continuous over the domain.

To be more concrete, consider the two factor, two good model with Leontief technology in Fig. 2. The isoquants are right angles and the isocost line connects the minimum points of the isoquants. For simplicity, shift the origin up along the  $v_1$  axis to the level of the  $f_2$  isoquant. Rescale inputs so that  $v_{22} = 1$  and  $w_1 = 1$ , as indicated in Fig. 2. The intersection of the  $f_1$  unit isoquant with the isocost line then occurs at a point  $(v_1, 1 - v_1)$ ,  $0 < v_1 < 1$ . The "foreign" unit isoquant  $f_1^*$  is a linear expansion from the new origin to  $(\Psi v_1, \Psi(1 - v_1))$ ,  $\Psi > 1$ . Define the distance between the home and foreign production functions for good 1 as the distance between minimum points on their isoquants. It follows that  $df = [(\Psi v_1 - v_1)^2 + (\Psi(1 - v_1) - (1 - v_1))^2]^{1/2} = v_1(\Psi - 1)\sqrt{2}$ . The  $w_1^*$  implied by the  $f_1^*$  isoquant is found by considering the similar triangles  $((1, 0), (\Psi v_1, 0), (\Psi v_1, \Psi(1 - v_1)))$  and  $((\Psi v_1, \Psi(1 - v_1)), (0, (\Psi(1 - v_1))), (0, 1/w_1^*))$ . It follows directly that  $w_1^* = \Psi(1 - v_1)/(1 - \Psi v_1)$ . The international distance be-

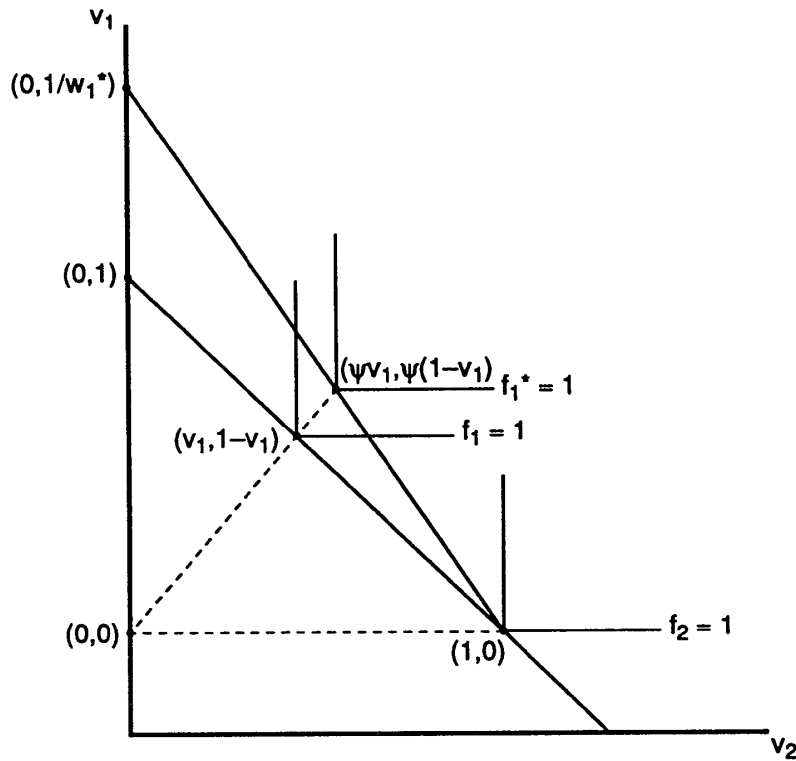


Fig. 2.

tween  $w_1$  and  $w_1^*$  is then  $dw_1 = 1 - w_1^* = (\Psi - 1) / \Psi(1 - v_1)$ . It follows that  $df = (v_1\sqrt{2})dw_1$ . Let  $dw_1$  be arbitrarily small:  $dw_1 = df / (v_1\sqrt{2}) < \varepsilon$ , for any  $\varepsilon > 0$ . It follows that  $df = (v_1\sqrt{2})dw < v_1\varepsilon\sqrt{2} \equiv \delta$ . Such a  $\delta$  can always be found for any arbitrarily small  $\varepsilon$ , and the mapping from this  $df$  to  $dw_1$  is continuous.

With exponential production functions,  $\phi_i$  must be monotonically increasing in  $df$ . If the assumption of exponential production functions is dropped,  $\phi_i$  would no longer necessarily be monotonic. Unit isoquants for good 1 can be sketched which result in  $dw_i$  falling as  $df$  rises. The results in this study are limited to exponential production functions, but would hold across other functional forms.

The slope of  $\phi_i$  indicates the sensitivity of  $dw_i$  to  $df$ . Compare  $\phi_i$  and  $\phi'_i$  in Fig. 3. The steeper  $\phi'_i$  implies that a larger factor price difference is created for the same  $df = \alpha$ :  $\phi'_i(\alpha) > \phi_i(\alpha)$ . Less flexibility in the production structure, reflecting more convex isoquants, is represented by  $\phi'_i$ . With  $\phi'_i$ , there are greater isocost adjustments and factor price differences as  $df$  increases. Steeper  $\phi_i$  occur as isoquants become more convex. At the other extreme,  $\phi_i$  would lie flat on the  $df$  axis if inputs were perfect substitutes.

#### 4. A SPECIFICATION OF THE DISTANCE MAPPING

This section presents a specification of the production model with two factors and two goods, the simplest general equilibrium model where FPE would hold if



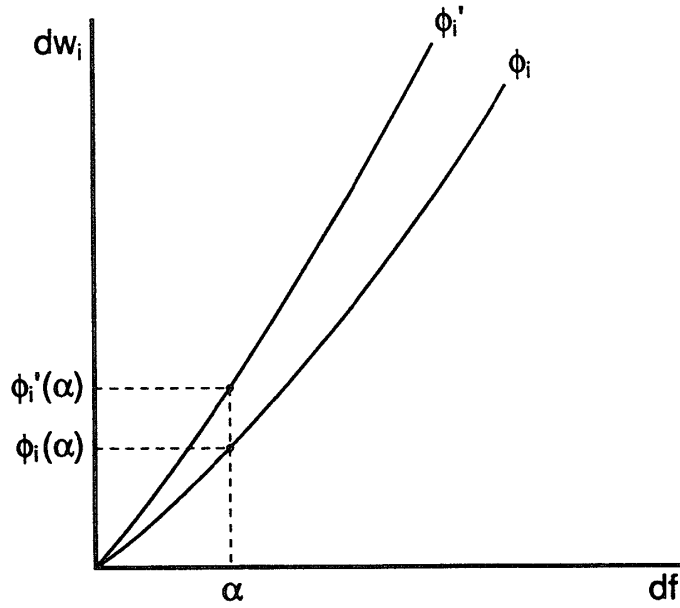


Fig. 3.

production functions were identical and the other sufficient conditions were met. Cobb–Douglas production functions are reported to provide a frame of reference. Specification of CES production functions, however, leads to  $\phi_i$  functions with quantitative properties similar to these reported in the Cobb–Douglas model. Other functional forms might lead to different quantitative insights.

A constant returns to scale production function for good 2 is assumed to be identical in the home and foreign countries:

$$x_2 = x_2^* = v_{12}^{0.25} v_{22}^{0.75} . \quad (11)$$

Production functions for good 1 in the home and foreign countries are:

$$x_1 = v_{11}^\gamma v_{21}^{1-\gamma} \quad \text{and} \quad x_1^* = v_{11}^{\gamma^*} v_{21}^{1-\gamma^*} . \quad (12)$$

Different coefficients  $\gamma$  and  $\gamma^*$  would imply different unit isoquants and different factor prices with free trade between the two countries.

Concentrate on the unit isoquants where  $1 = p_1 = p_2 = x_1^* = x_1 = x_2^* = x_2$ . Where  $a_{ij}$  is the amount of factor  $i$  used per unit of good  $j$ ,  $a_{12} = a_{22}^{-3}$  from (12) along the unit isoquant for good 2. For good 1,  $a_{11} = a_{21}^{(\gamma-1)/\gamma}$  at home and  $a_{11} = a_{21}^{(\gamma^*-1)/\gamma^*}$  abroad. Using these unit isoquants along with the isocost lines and the condition of cost minimization, the factor mix terms can be written as functions of the relative price of factors:

$$a_{21} = [((1-\gamma)/\gamma)(w_1/w_2)]^\gamma \quad \text{and} \quad a_{22} = [3(w_1/w_2)]^{0.25} \quad (13)$$

In the foreign country,  $a_{22}^*$  is similarly expressed with  $\gamma^*$ . The implied factor prices are

TABLE 1. Specification results.

$\gamma$	$df$	$w_1$	$\% \Delta w_1$	$w_2$	$\% \Delta w_2$
0.85	0.054	0.679	19.1%	0.538	-5.6%
0.80	0.024	0.620	8.8%	0.554	-2.8%
0.78	0.014	0.599	5.1%	0.560	-1.8%
0.76	0.005	0.579	1.6%	0.567	-0.5%
0.75	0	0.570	—	0.570	—
0.74	0.003	0.561	-1.6%	0.573	0.5%
0.72	0.011	0.542	-4.9%	0.579	1.6%
0.70	0.018	0.526	-7.7%	0.585	2.6%
0.65	0.032	0.486	-14.7%	0.601	5.4%

$$w_1 = 0.105 w_2^{-3} \quad \text{and} \quad w_2 = 0.105^{\gamma/(4\gamma-1)} \sigma_\gamma^{1/(4\gamma-1)} \quad (14)$$

where  $\rho_\gamma = ((1-\gamma)/\gamma)^{\gamma-1} + ((1-\gamma)/\gamma)^\gamma$ . Again,  $\gamma^*$  would be used to express foreign factor prices.

Model specifications are presented in Table 1. Suppose  $\gamma = \gamma^* = 0.75$  and FPE occurs as in the middle row of Table 1. Factor 1 (2) is used intensively in industry 1 (2). Factor prices are then  $w_i = w_i^* = 0.570$ ,  $i = 1, 2$ .

In the foreign country, let  $\gamma^*$  remain at 0.75 and  $w_1^*$  and  $w_2^*$  both at 0.570. In the first column of Table 1,  $\gamma$  is varied to create a range of domestic factor price adjustments. When  $\gamma$  is 0.76, for instance,  $w_1 = 0.579$ . Relative to the foreign country, the home country would then have a production function in sector 1 intensive in factor 1. A higher price of factor 1 in the home country occurs, a result similar to that of Bardhan (1965).

The distance  $df$  in Table 1 is calculated by integrating over  $v_2$  from 1 to 2 as in (6). When  $\gamma$  is 0.76, the distance measure between production functions is  $df = 0.005$ . Chipman (1991) calculates an analogous measure of similarity between Cobb–Douglas production functions. Note that  $w_1$  is only 1.6% higher in the home country than in the foreign country when  $\gamma = 0.76$ .

Continuity of the function  $\phi_1$  may be apparent from the first three columns of Table 1. Choosing a  $\gamma$  closer to 0.76, for instance, would result in a  $w_1$  closer to 0.573 and a  $df$  closer to 0.010. Suppose  $\gamma$  is chosen to result in a  $w_1$  arbitrarily close to 0.573. In other words,  $w_1$  is in the open interval  $(0.573 - \varepsilon, 0.573 + \varepsilon)$  for any  $\varepsilon > 0$ . For notation,  $\phi_1(df^-) = 0.573 - \varepsilon$  and  $\phi_1(df^+) = 0.573 + \varepsilon$ . For this particular  $\gamma$ ,  $df$  is in the open interval  $(df^-, df^+)$ . If there is a  $\delta$  such that  $(df - \delta, df + \delta)$  is a subset of  $(df^-, df^+)$ ,  $\phi_i$  would be continuous at  $df = 0.005$ . Given the exponents in (13) and (14), solving for this  $\delta$  is not a straightforward task, but for any  $\varepsilon$  an appropriate  $\delta$  could be chosen.

Moving up the first column in Table 1, increments of 0.02 in  $\gamma$  lead to  $\gamma = 0.80$ , a substantial difference from the foreign country's production function. Here,  $df = 0.024$  and  $w_1$  has risen 8.8% from its base value. For  $\gamma = 0.80$ ,  $w_2$  would be 0.554. There is thus a greater percentage change in the price of the factor used

intensively in the industry whose production function is different. Generalizing this result to models with more factors and more goods would be complicated by the vagueness of the concept of factor intensity.

With the jump to  $\gamma=0.85$  in the top row of Table 1, the percentage change in  $w_1$  rises to 19.1%. Moving down Table 1 from  $\gamma=0.75$ , the production of good 1 in the home country becomes intensive in factor 2. The percentage adjustment in  $w_1$  remains larger than the percentage adjustment in  $w_2$ . In Fig. 1, the isocost line has to rotate around the stationary unit isoquant for good 2.

##### 5. GENERALIZING RESULTS FROM THE COBB-DOUGLAS SPECIFICATION

Cobb–Douglas production functions represent more convex isoquants and less flexibility than might typically be the case in the long run for many industries. Specification of CES production functions allows variation in the partial elasticity of substitution. Percentage changes in factor prices with the elasticity of substitution ranging from 0.5 to 2 turn out to be similar to the Cobb–Douglas results in Table 1, where the elasticity of substitution equals one.

The common international technical coefficients for good 2 production also makes some difference in the characteristics of the  $\phi_i$  mapping. Sensitivity analysis with variation in these coefficients between  $v_{12}^{0.1}v_{22}^{0.9}$  and  $v_{12}^{0.4}v_{22}^{0.6}$  with a similar range for differences in  $\gamma$  and  $\gamma^*$  produces variation in international factor prices similar to those reported in Table 1.

With many inputs and many goods, differences in any particular production coefficient across countries would result in smaller differences in factor prices than those reported in Table 1. Increasing the dimensions of the model, in other words, would flatten  $\phi_i$  when only one production function coefficient varies across countries. When the number of different production functions across countries increases, the degrees of freedom leading to  $dw_i$  would increase. As more production functions differ across countries, the change in a particular  $\phi_i$  would depend on the “direction” of differences.

##### 6. CONCLUSION

When a country opens itself to international trade or imposes protection, projected degrees of factor price adjustment depend on a number of underlying technical conditions. The present note makes the point that international differences in production functions alone are not reason enough to abandon the general result that free trade would cause factor prices to become more equal across countries.

A related result occurs when there are more factors than international markets. Factor price equalization does not hold since international differences in factor endowments would result in different sets of factor prices. Nevertheless, elasticities describing the effect of factor endowment changes on factor prices are found to

be nearly zero in Thompson (1990). Prices of similar factors must then be close together across freely trading competitive economies, a result called near factor price equalization.

Tests of factor proportions trade theory are somewhat hamstrung by the assumption of identical production functions across countries. General equilibrium models of production and trade can certainly be developed and applied if production functions differ internationally. The condition of identical production functions across countries is not necessary to specify and utilize a coherent microeconomic general equilibrium theory of production and trade. Given the limited ability to differentiate between categories of productive factors, it is sensible to proceed by allowing the inevitable differences in estimated production functions.

The main thrust of FPE and the Stolper-Samuelson theorem is that a move to free trade would tend to equalize the international functional distribution of income. This notion is not grossly diluted by international differences in production functions. The present paper puts forth the hypothesis that anticipated differences in production functions would not produce large international differences in factor prices when factor price equalization would otherwise hold. It remains an empirical issue what share of the observed international differences in factor prices can be attributed to a lack of free international trade or domestic conditions, and how much can be attributed to international differences in production functions.

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